



Different Tropospheric Mapping Functions and Cut off Angles Investigated by Processing VLBI CONT05 Sessions

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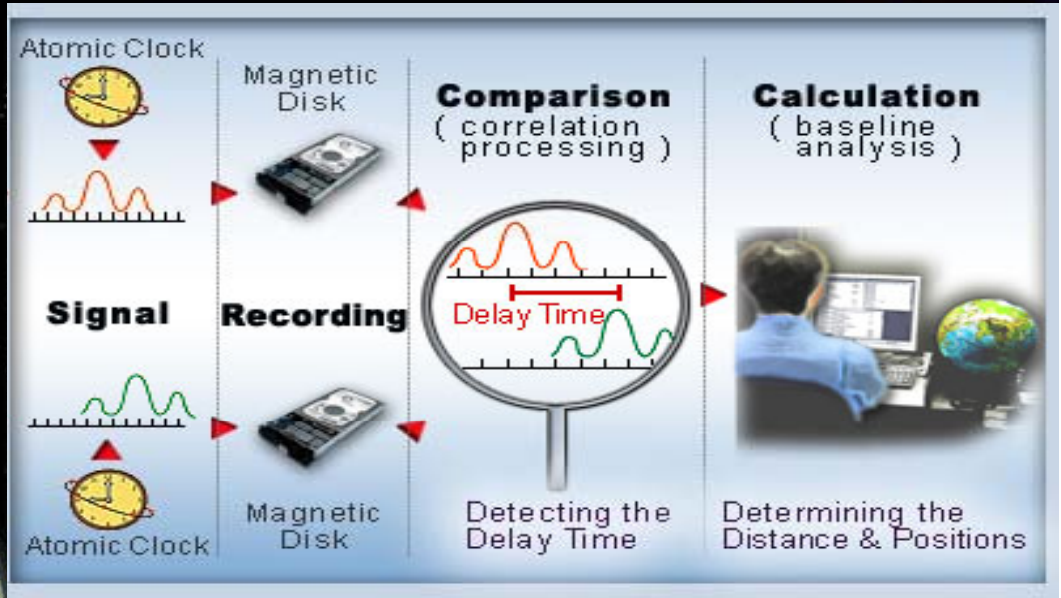
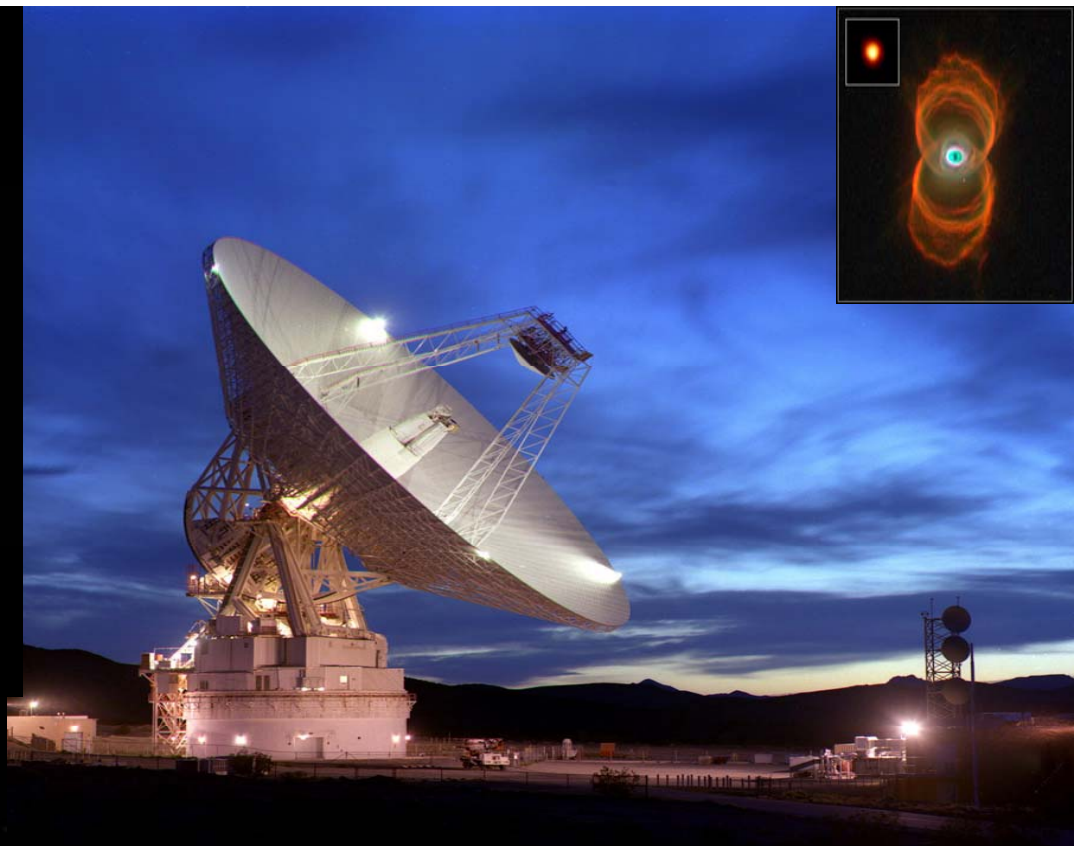
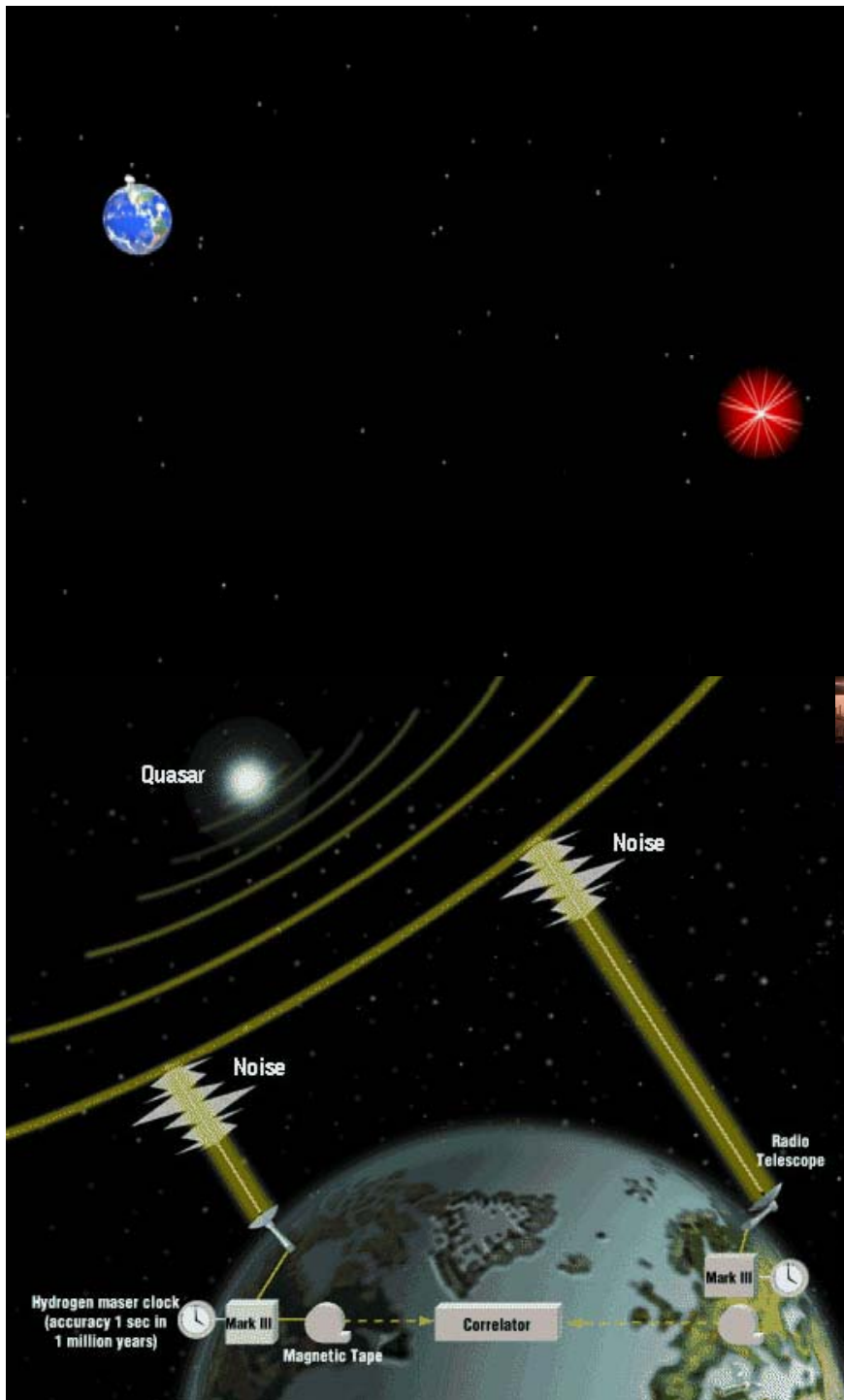
Johannes Boehm¹

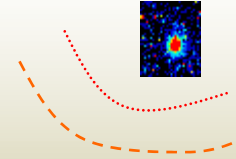
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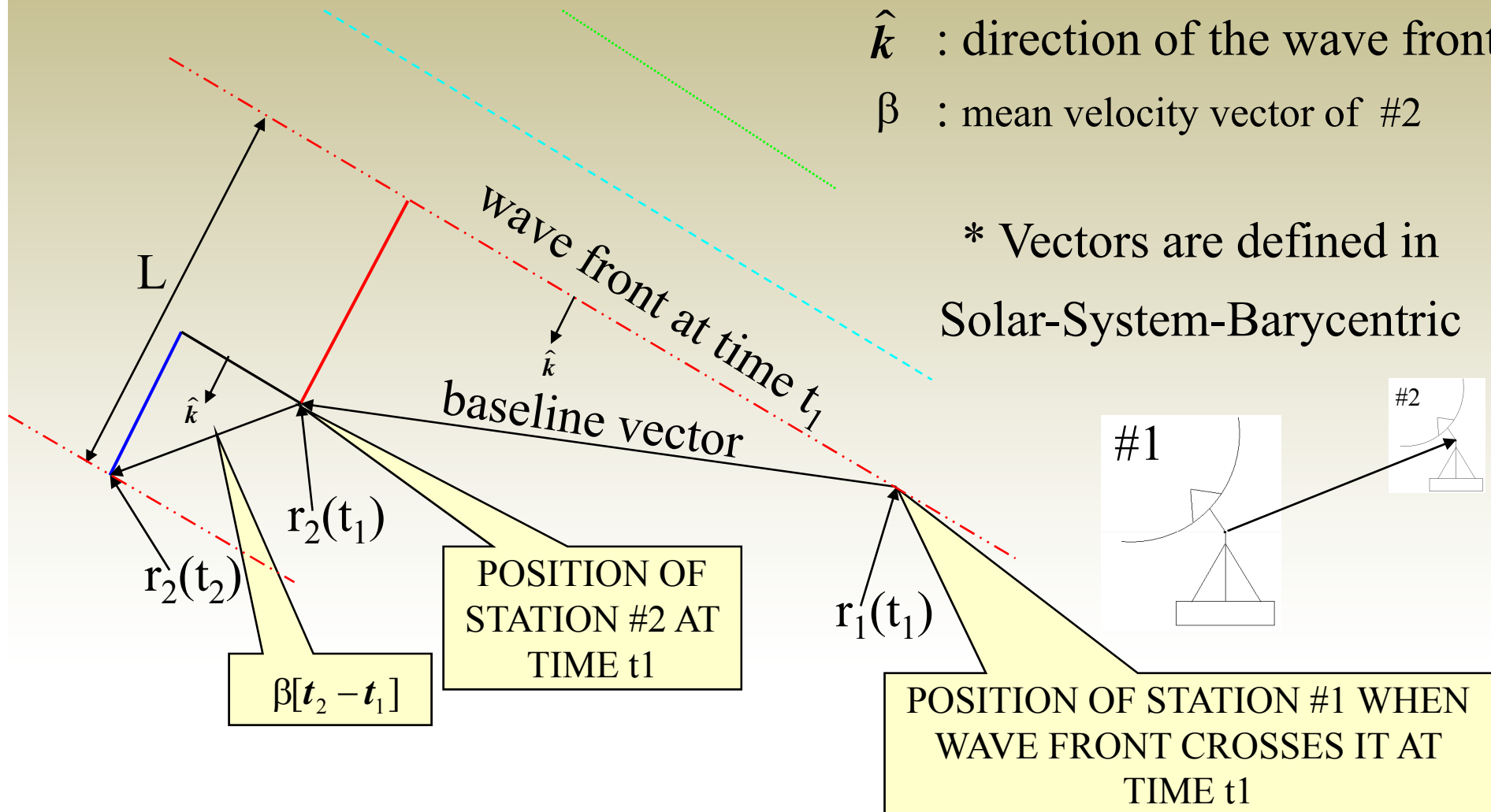
VLBI GEOMETRIC MODEL

$$c(\tau_{\text{obs}} - (\tau_{\text{clock}} + \tau_{\text{trop}} + \tau_{\text{ionos}} + \tau_{\text{rel}})) = c \cdot (t_2 - t_1) = \hat{k} [r_2(t_1) - r_1(t_1)] + \hat{k} \beta [t_2 - t_1]$$

\hat{k} : direction of the wave front

β : mean velocity vector of #2

* Vectors are defined in Solar-System-Barycentric





VLBI TROPOSPHERE MODEL

Total Delay = Ionospheric Delay + Neutral Delay

Zenith Neutral Delay = Zenith Hydrostatic Delay + Zenith Wet Delay

$$\Delta L(e) = ZHD.mf_h(e) + ZWD.mf_w(e)$$

$\Delta L(e)$: Zenith neutral path delay

$mf_{h,w}$: Hydrostatic, wet tropospheric mapping functions

(NMF, GMF, IMF, VMF1)

$ZHD = f(\varphi, H, P)$: Zenith Hydrostatic delay

ZWD = Estimated in VLBI analysis

by piecewise linear function : Zenith wet delay

$$\tau_{troposphere} = -\frac{1}{c}(\Delta L_2(e) - \Delta L_1(e)) \quad (\text{for the station 1 and 2})$$



TROPOSPHERIC MAPPING FUNCTIONS

$$m_{h,w}(e) = \frac{1 + \frac{a_i}{1 + \frac{b_i}{1 + \frac{c_i}{1 + \dots}}}}{\sin(e) + \frac{a_i}{\sin(e) + \frac{b_i}{\sin(e) + \frac{c_i}{\sin(e) + \dots}}}}$$

e : Elevation cut off angle

$a_i, b_i, c_i, \dots = f(\varphi, H, \text{doy}, t, \alpha, \dots)$

φ : station latitude

H : station orthometric height

doy : day of year

P : surface total pressure

t : surface temperature

α : temperature lapse rate

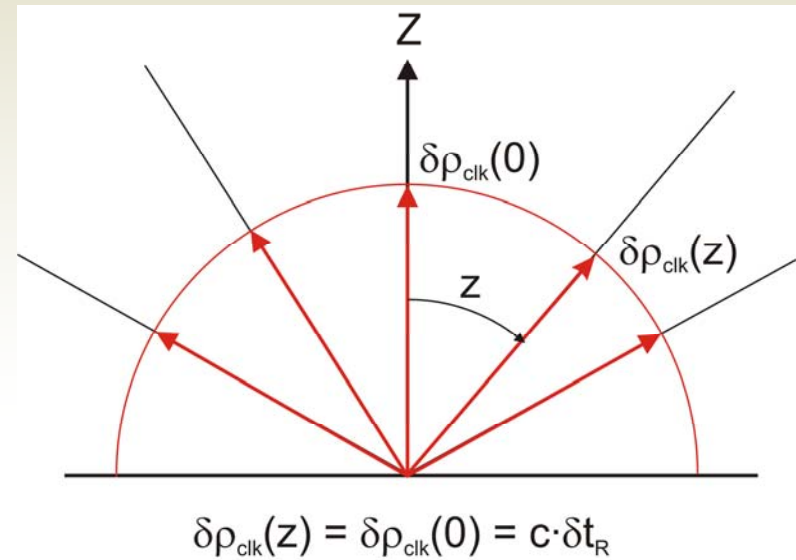
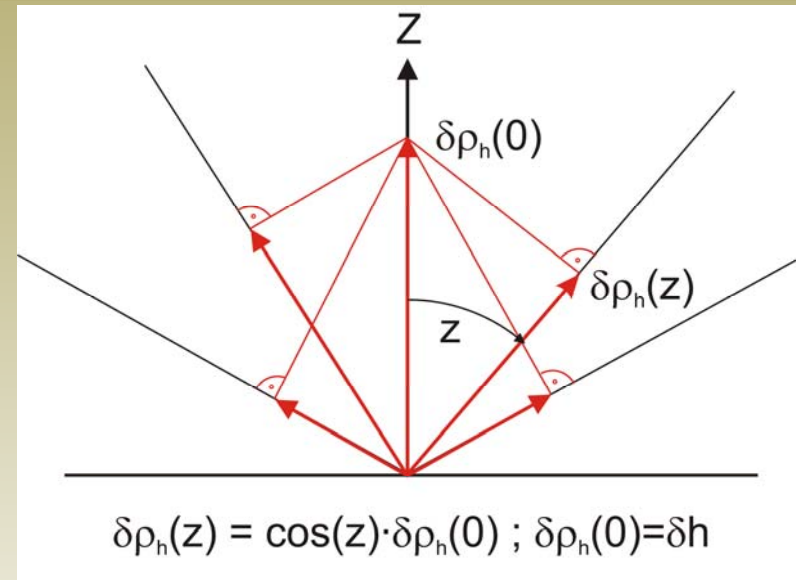
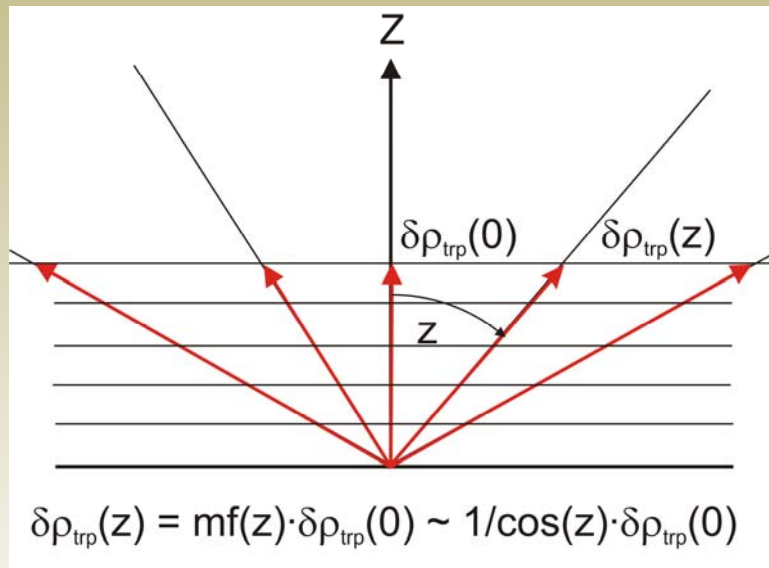
Niell Mapping Function

Isobaric Mapping Function

Vienna Mapping Function

Some other mapping functions:

Chao, Ifadis, Davis, MTT, B&E, F&K, UNBabc, UNBab



Different Tropospheric Mapping Functions and Cut off Angles Investigated by Processing VLBI CONT05 Sessions

VLBI CONT05 STATIONS

CONT05 was a two-week campaign of continuous VLBI sessions, scheduled for observing during September 2005.



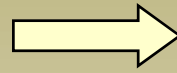
The plan for the CONT05 campaign is to acquire state of the art VLBI data over a two-week period to demonstrate the highest accuracy of which VLBI is capable.



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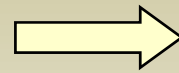
Regression function of the baseline length repeatabilities and fitting a curve

$$\sigma = \sqrt{\frac{\sum_{i=1}^n (L_i - L_0)^2}{n-2}}$$



Formal errors as
baseline length repeatabilities

$$y = a^2 + b^2 \text{ppb}^2 L^2$$



Regression function for
baseline length
repeatabilities

LSM Application

$$y = \begin{bmatrix} r_{MSS_1}^2 \\ r_{MSS_2}^2 \\ \vdots \\ r_{MSS_n}^2 \end{bmatrix}; A = \begin{bmatrix} 1 & \text{ppb}^2 L_1^2 \\ 1 & \text{ppb}^2 L_2^2 \\ \vdots & \vdots \\ 1 & \text{ppb}^2 L_n^2 \end{bmatrix}; x = \begin{bmatrix} a^2 \\ b^2 \end{bmatrix}; W = \begin{bmatrix} 1/s_1^2 & & & \\ & 1/s_2^2 & & \underline{0} \\ & & \ddots & \\ & & & \underline{0} \\ & & & & 1/s_n^2 \end{bmatrix}$$

$$x = (A^T W A)^{-1} A^T W y$$



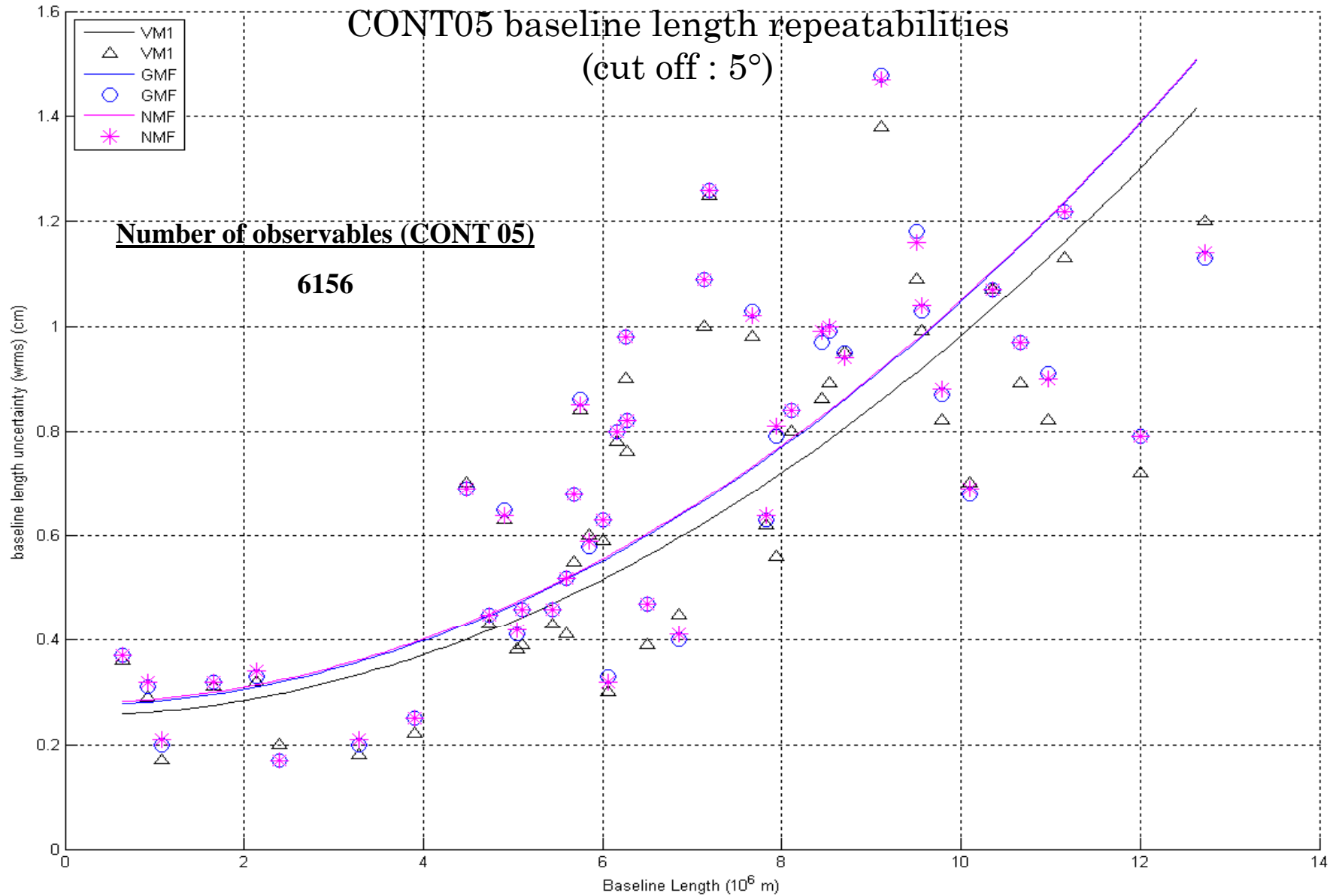
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Values of the estimated parameters by LSM

<i>Mapping Functions</i>	<i>Parameters of the function for different cut off angles</i>									
	<i>5° (6156)</i>		<i>6°(6028)</i>		<i>7°(5907)</i>		<i>8°(5818)</i>		<i>9°(5646)</i>	
	<i>a (cm)</i>	<i>b</i>	<i>a (cm)</i>	<i>b</i>	<i>a (cm)</i>	<i>b</i>	<i>a (cm)</i>	<i>b</i>	<i>a (cm)</i>	<i>b</i>
<i>VMI</i>	0.505	0.853	0,515	0,817	0,517	0,801	0,523	0,796	0,510	0,836
<i>GMF</i>	0,524	0,879	0,521	0,844	0,521	0,823	0,522	0,806	0,512	0,844
<i>NMF</i>	0,528	0,879	0,520	0,844	0,521	0,826	0,522	0,808	0,512	0,845
<i>Mapping Functions</i>	<i>10°(5502)</i>		<i>12°(5207)</i>		<i>15°(4730)</i>		<i>20°(3906)</i>		<i>30°(2491)</i>	
	<i>a (cm)</i>	<i>b</i>	<i>a (cm)</i>	<i>b</i>	<i>a (cm)</i>	<i>b</i>	<i>a (cm)</i>	<i>b</i>	<i>a (cm)</i>	<i>b</i>
	<i>VMI</i>	0,501	0,859	0,489	0,927	0,428	1,078	0,404	1,229	0,657
<i>GMF</i>	0,500	0,866	0,488	0,931	0,426	1,081	0,403	1,229	0,656	1,542
<i>IMF</i>	0,500	0,867	0,489	0,931	0,428	1,081	0,404	1,228	0,655	1,543

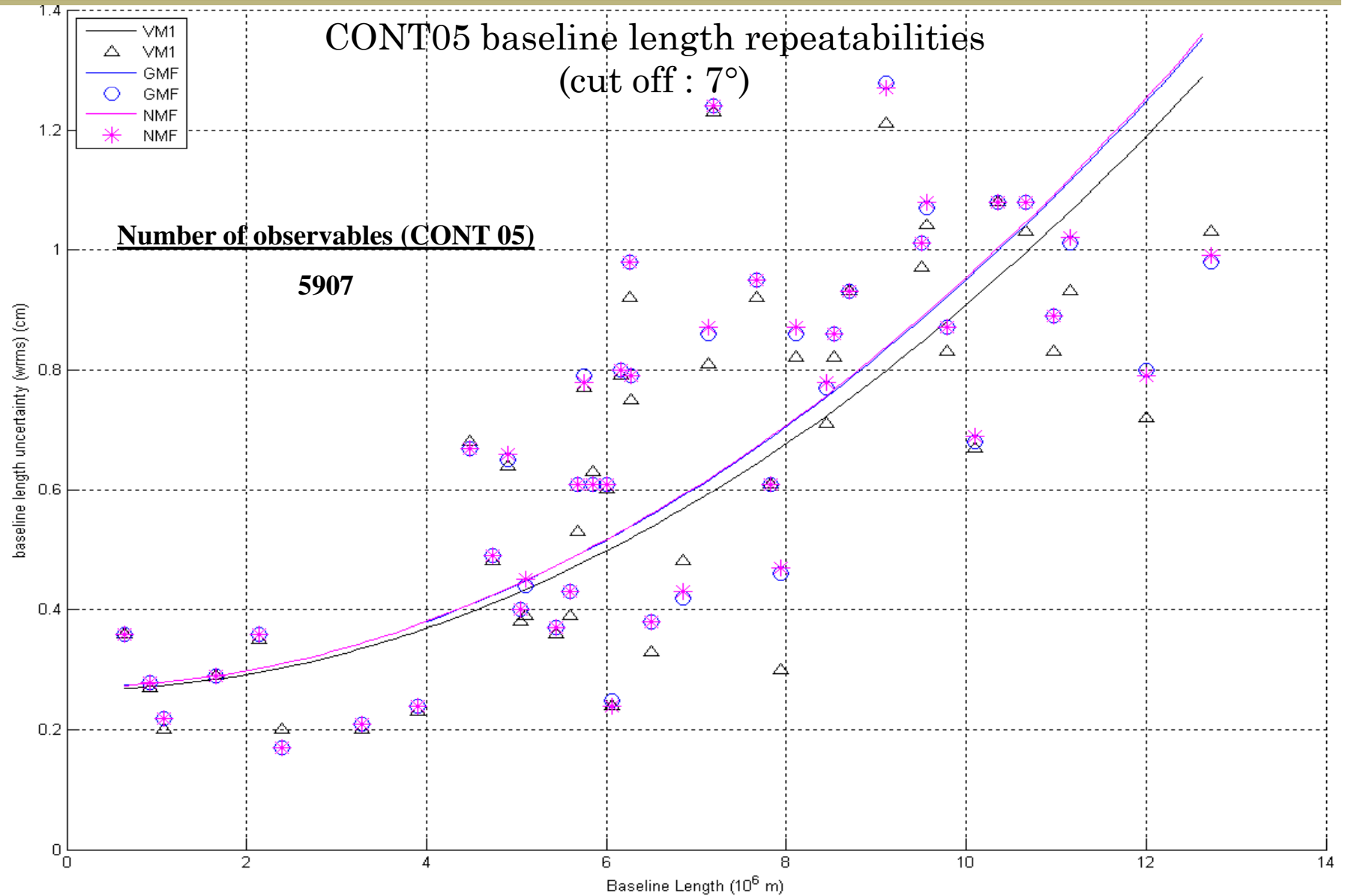


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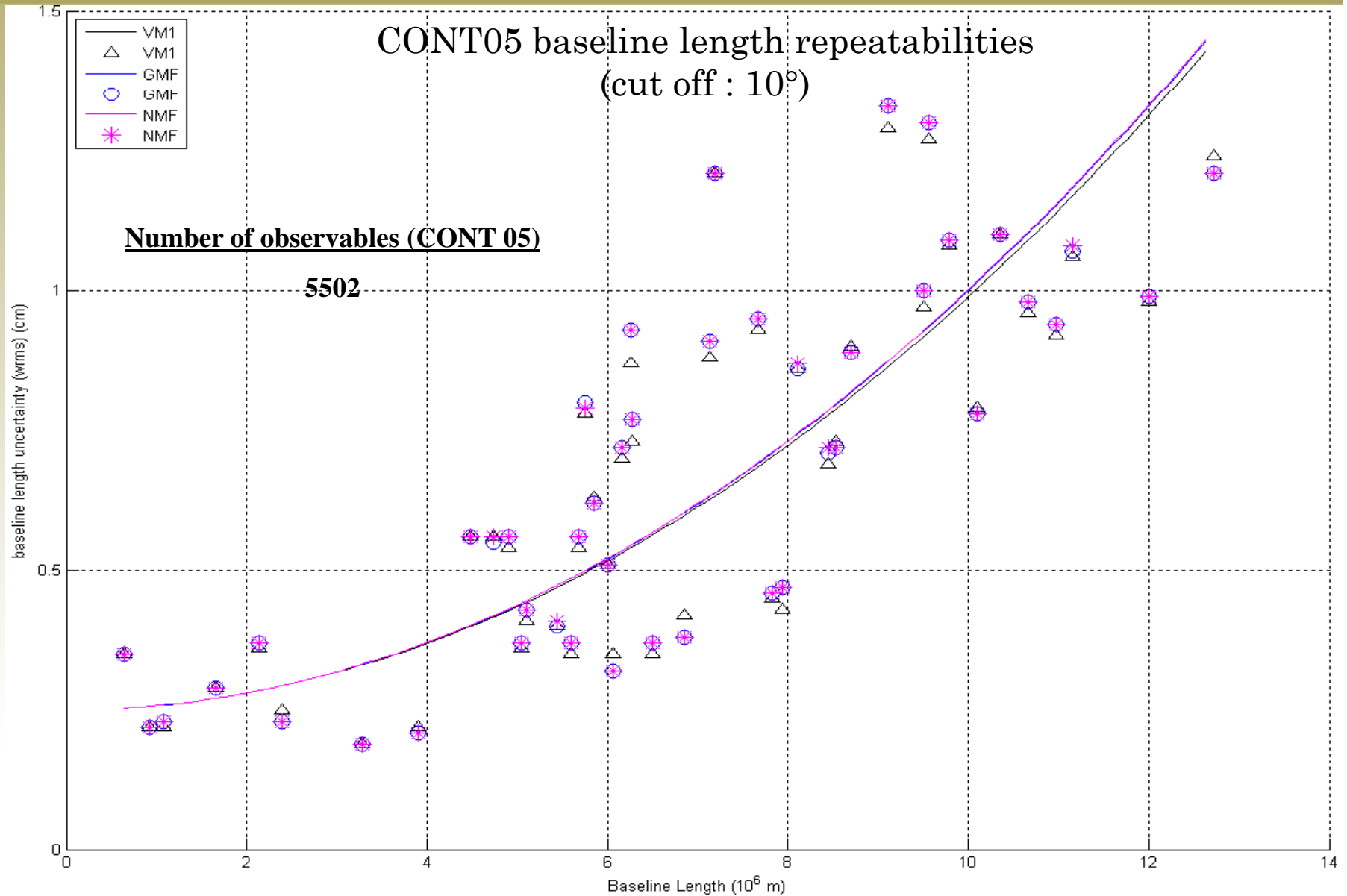


Different Tropospheric Mapping Functions and Cut off Angles Investigated by Processing VLBI CONT05 Sessions



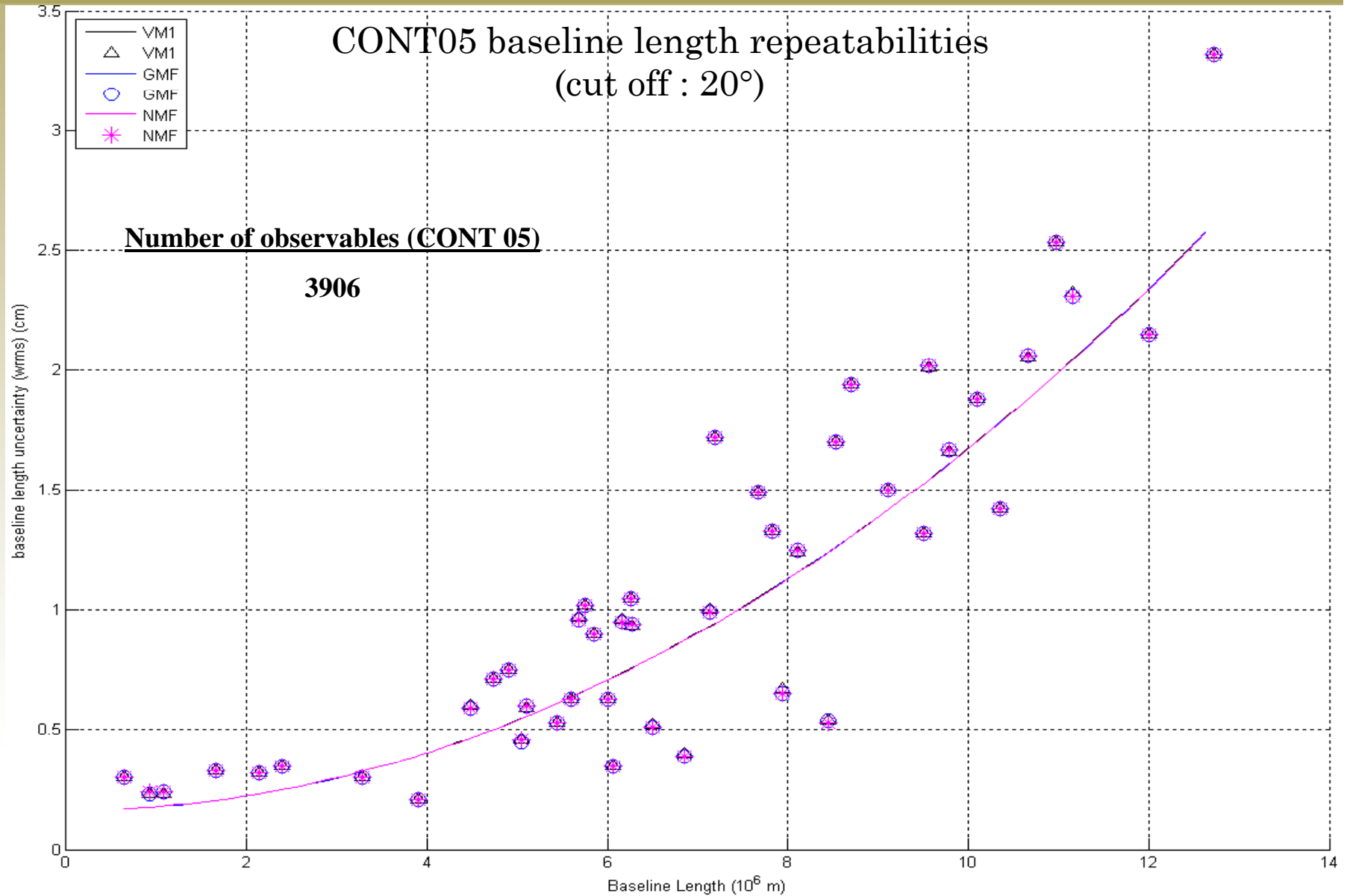


Different Tropospheric Mapping Functions and Cut off Angles Investigated by Processing VLBI CONT05 Sessions





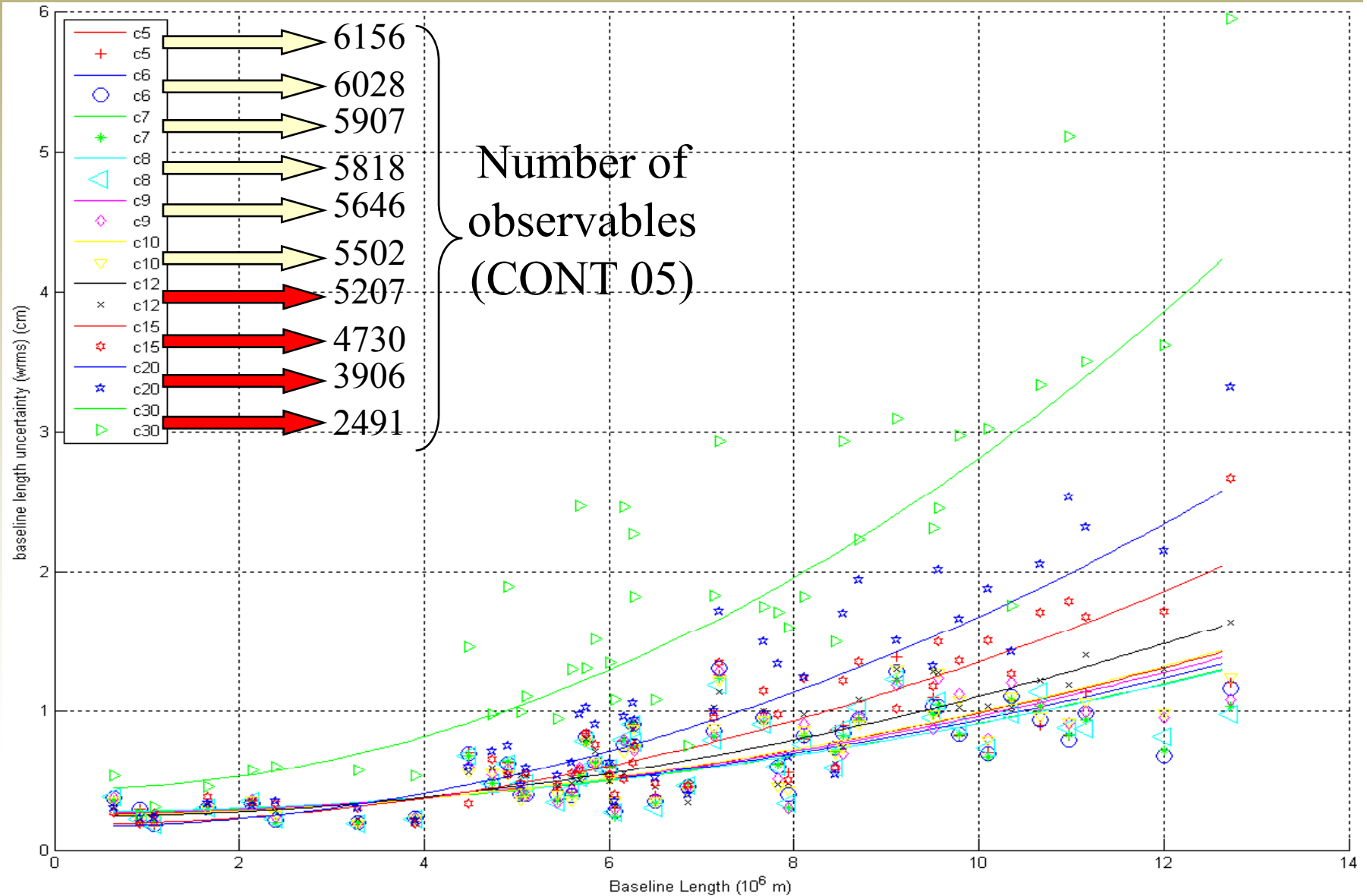
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Different Tropospheric Mapping Functions and Cut off Angles Investigated by Processing VLBI CONT05 Sessions

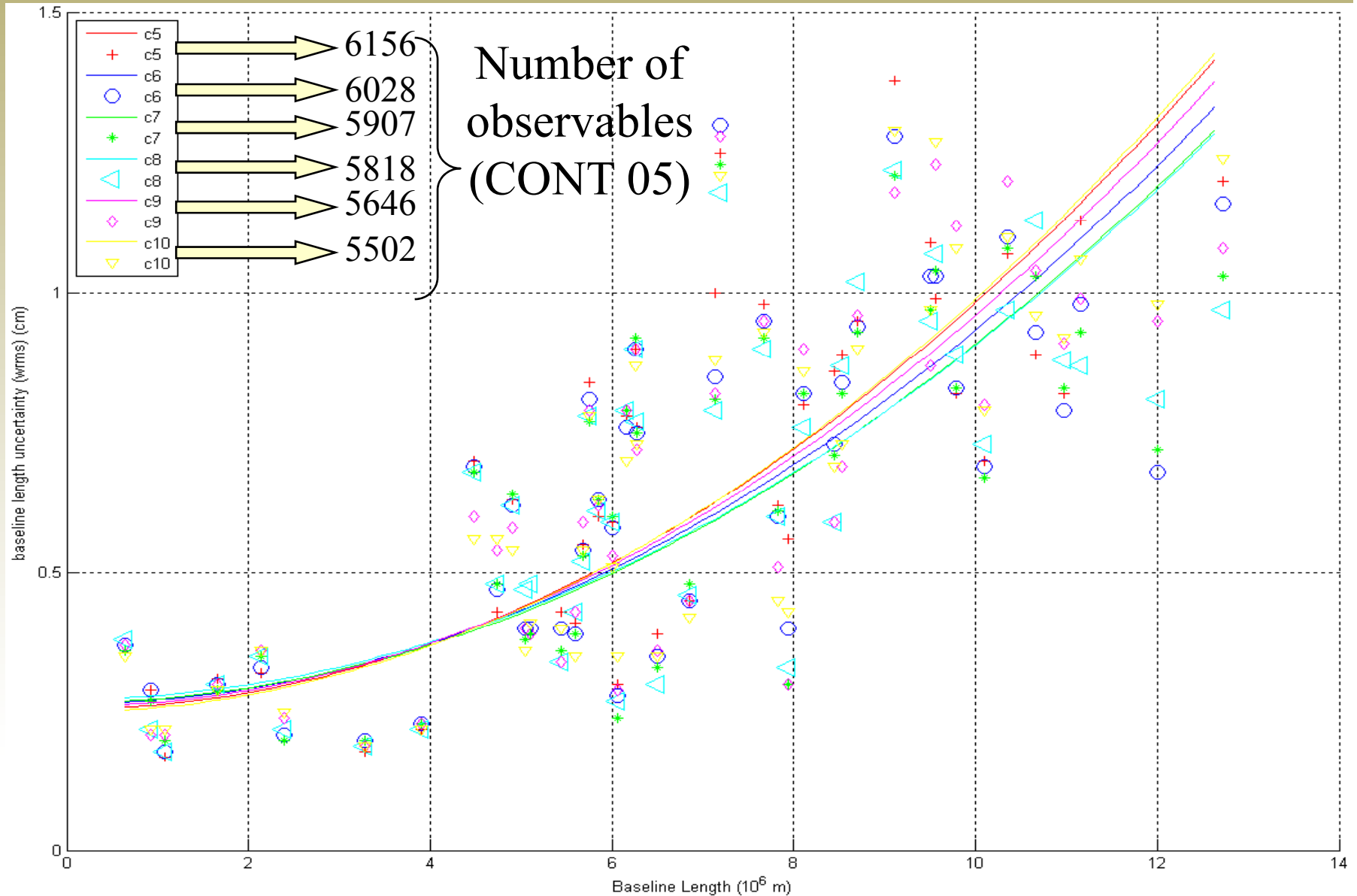
CONT05 baseline length repeatabilities (VMF1)





Different Tropospheric Mapping Functions and Cut off Angles Investigated by Processing VLBI CONT05 Sessions

CONT05 baseline length repeatabilities (VMF1)





Values of the estimated parameters by LSM

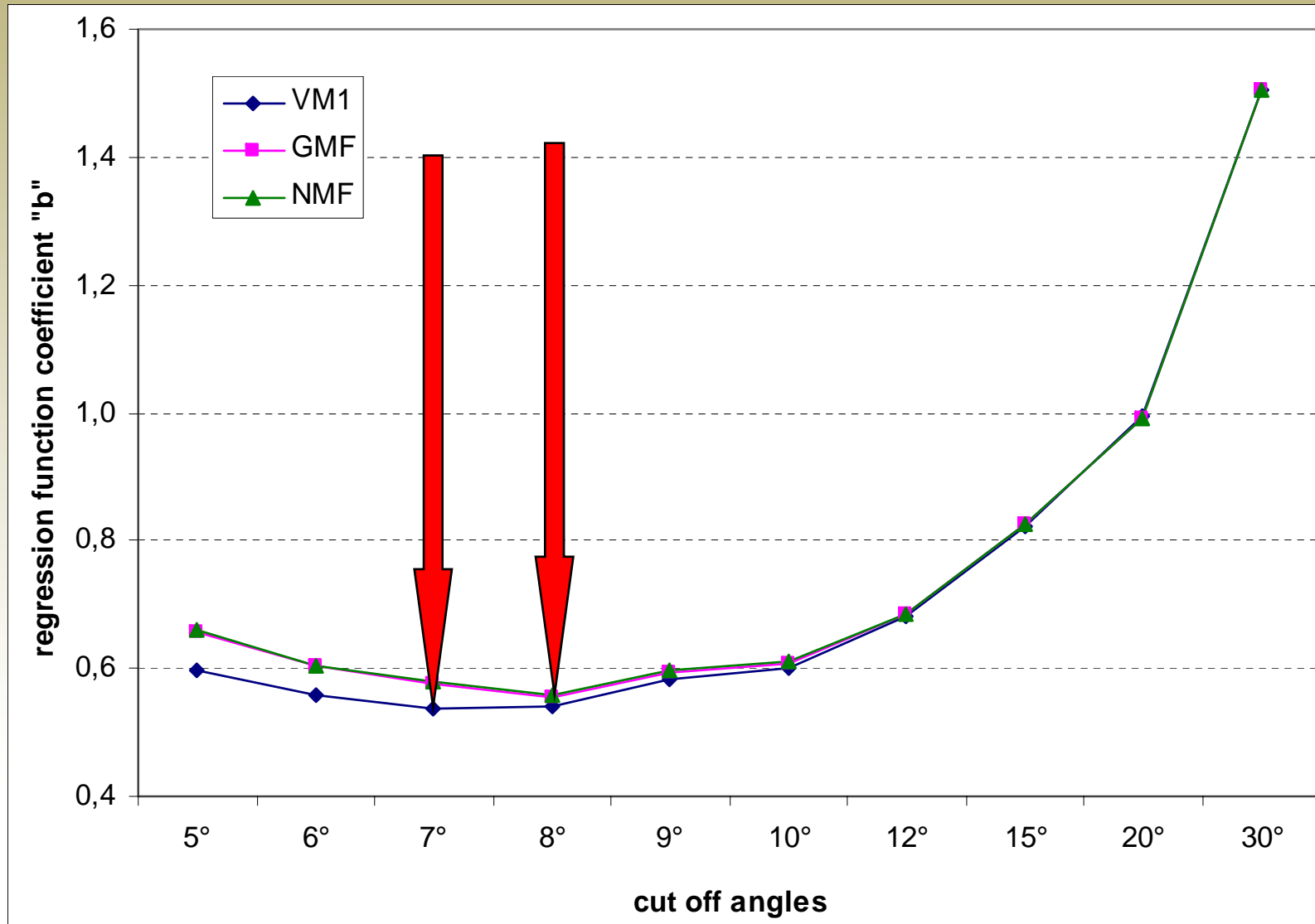
Parameter “a“ fixed to 0.5 cm

Mapping Functions	<i>Parameters of the function for different cut off angles</i>									
	5 5°(6156)		3 6°(6028)		1 7°(5907)		2 8°(5818)		4 9°(5646)	
	<i>a</i> (cm)	<i>b</i>	<i>a</i> (cm)	<i>b</i>	<i>a</i> (cm)	<i>b</i>	<i>a</i> (cm)	<i>b</i>	<i>a</i> (cm)	<i>b</i>
<i>VMI</i>	0,5	0,597	0,5	0,559	0,5	0,537	0,5	0,540	0,5	0,582
<i>GMF</i>	0,5	0,657	0,5	0,605	0,5	0,577	0,5	0,554	0,5	0,595
<i>NMF</i>	0,5	0,660	0,5	0,605	0,5	0,580	0,5	0,558	0,5	0,597
Mapping Functions	6 10°(5502)		12°(5207)		15°(4730)		20°(3906)		30°(2491)	
	<i>a</i> (cm)	<i>b</i>	<i>a</i> (cm)	<i>b</i>	<i>a</i> (cm)	<i>b</i>	<i>a</i> (cm)	<i>b</i>	<i>a</i> (cm)	<i>b</i>
	<i>VMI</i>	0,5	0,600	0,5	0,680	0,5	0,823	0,5	0,994	0,5
<i>GMF</i>	0,5	0,610	0,5	0,685	0,5	0,824	0,5	0,993	0,5	1,505
<i>IMF</i>	0,5	0,611	0,5	0,686	0,5	0,826	0,5	0,992	0,5	1,506



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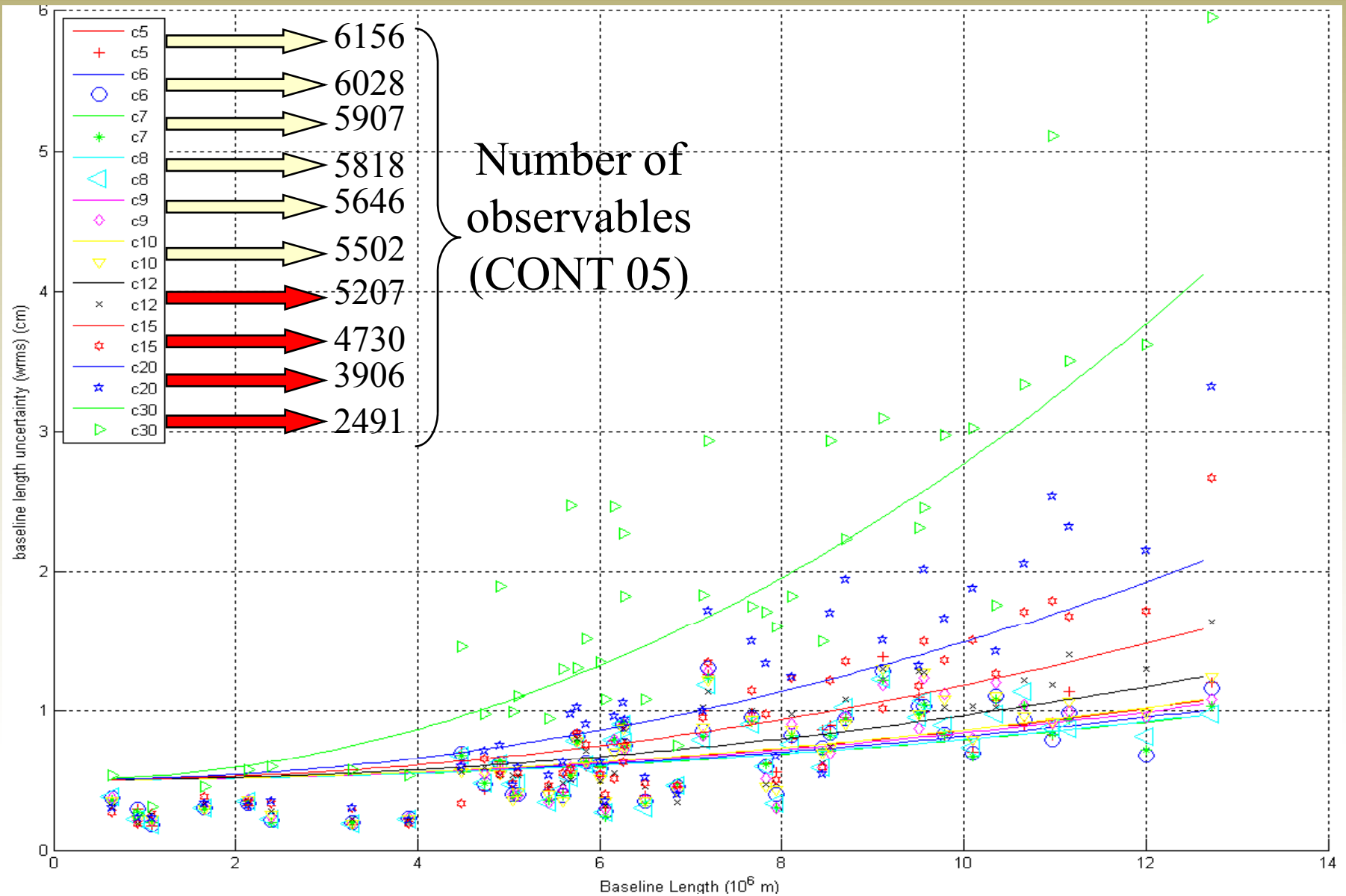
Comparison of the parameter “b”





Different Tropospheric Mapping Functions and Cut off Angles Investigated by Processing VLBI CONT05 Sessions

CONT05 baseline length repeatabilities (VMF1) Parameter "a" fixed to 0.5 cm





Simulation Formula

$\Delta\tau$: Observed group delay is simulated

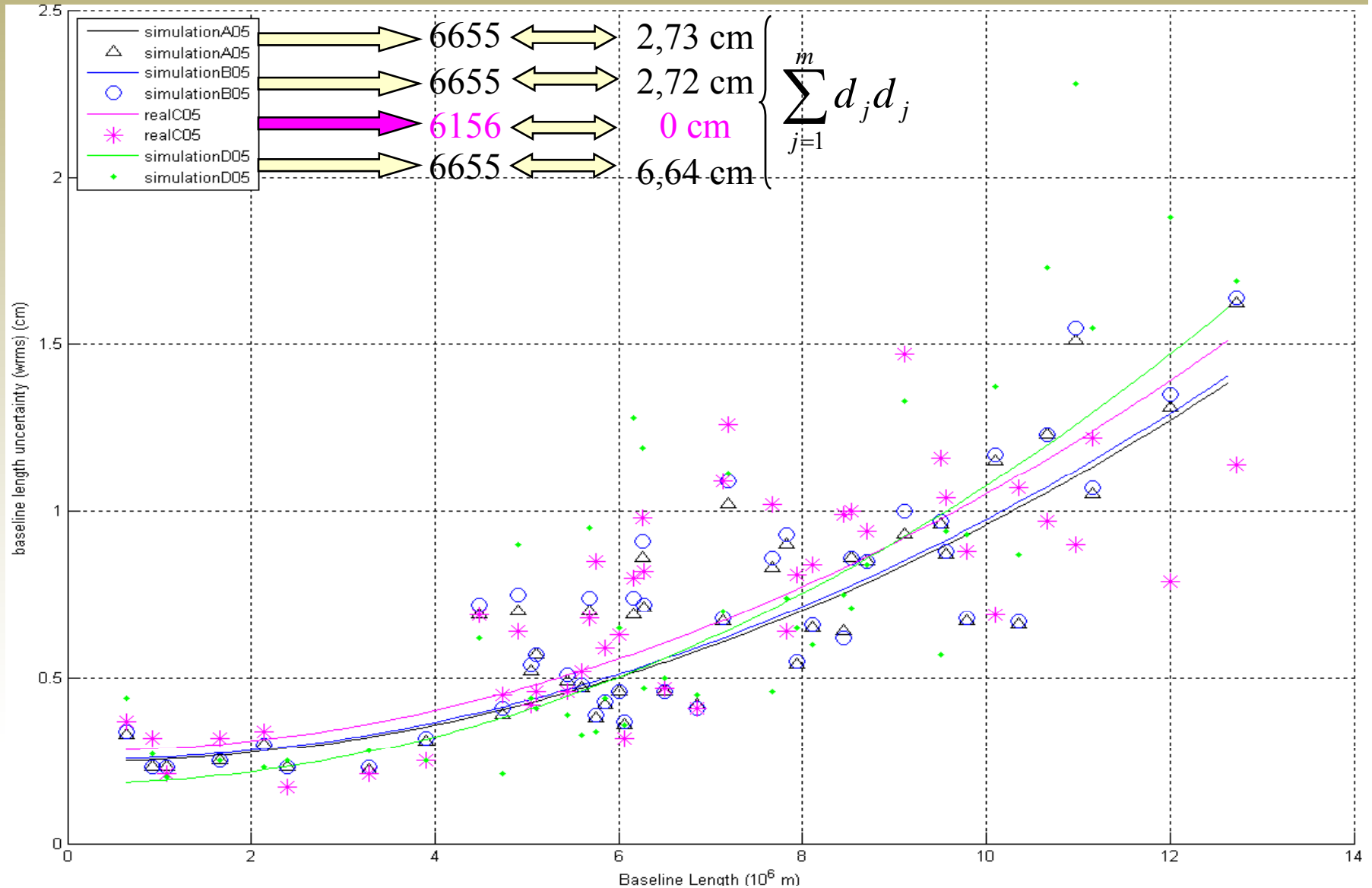
$$\Delta\tau = \Delta\tau_{\text{computed}} + (\text{WZD}_2 \text{ mfw}_2(e) + \text{cl}_2) - (\text{WZD}_1 \text{ mfw}_1(e) + \text{cl}_1) + \text{wn}_{\text{bsl}(1-2)}$$

$$\sum_{j=1}^m (\text{rep}_{\text{real}(j)} - \text{rep}_{\text{simulated}(j)})^2 \Rightarrow \min$$



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Comparison of baseline length repeatabilities derived from simulated and real CONT05 NGS files





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Simulation Results

Parameters	Simulations					
	1 st Simulation (A05)		2 nd Simulation (B05)		3 rd Simulation (D05)	
white noise	8psec (2.4 mm)		12psec (3.6mm)		8psec (2.4mm)	
predicted clock	1e-15@15min		1e-15@15min		1e-15@15min	
	Station	PSD (psec ² /sec)	Station	PSD (psec ² /sec)	Station	PSD (psec ² /sec)
predicted wet zenith delay	HARTRAO	0.1	HARTRAO	0.1		
	KOKEE	0.8	KOKEE	0.8		
	TSUKUB32	0.6	TSUKUB32	0.6	All stations	0.5
	The rest of all stations	0.5	The rest of all stations	0.5		



Conclusions

- Similar baseline uncertainty values for cut off angles 5 to 10 degrees but not for 12 to 30 degrees.
- In spite of the small differences, VM1 gives always the best results.
- If the same amount of observables for simulations with the real ones, cut off angle 7 gives approximately the best outcomes.
- It has been succeeded to create overlapped simulation outcomes with the real ones for cut off angle 7 degree.



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Outlook

- No need to observe quasars below the cut off angle 7 unless the wet zenith delay parameters will be measured accurately and the related models will be improved.
- Future simulations should use the turbulence model for the wet zenith delays.
- Down-weighting of low elevation observations should be tested.

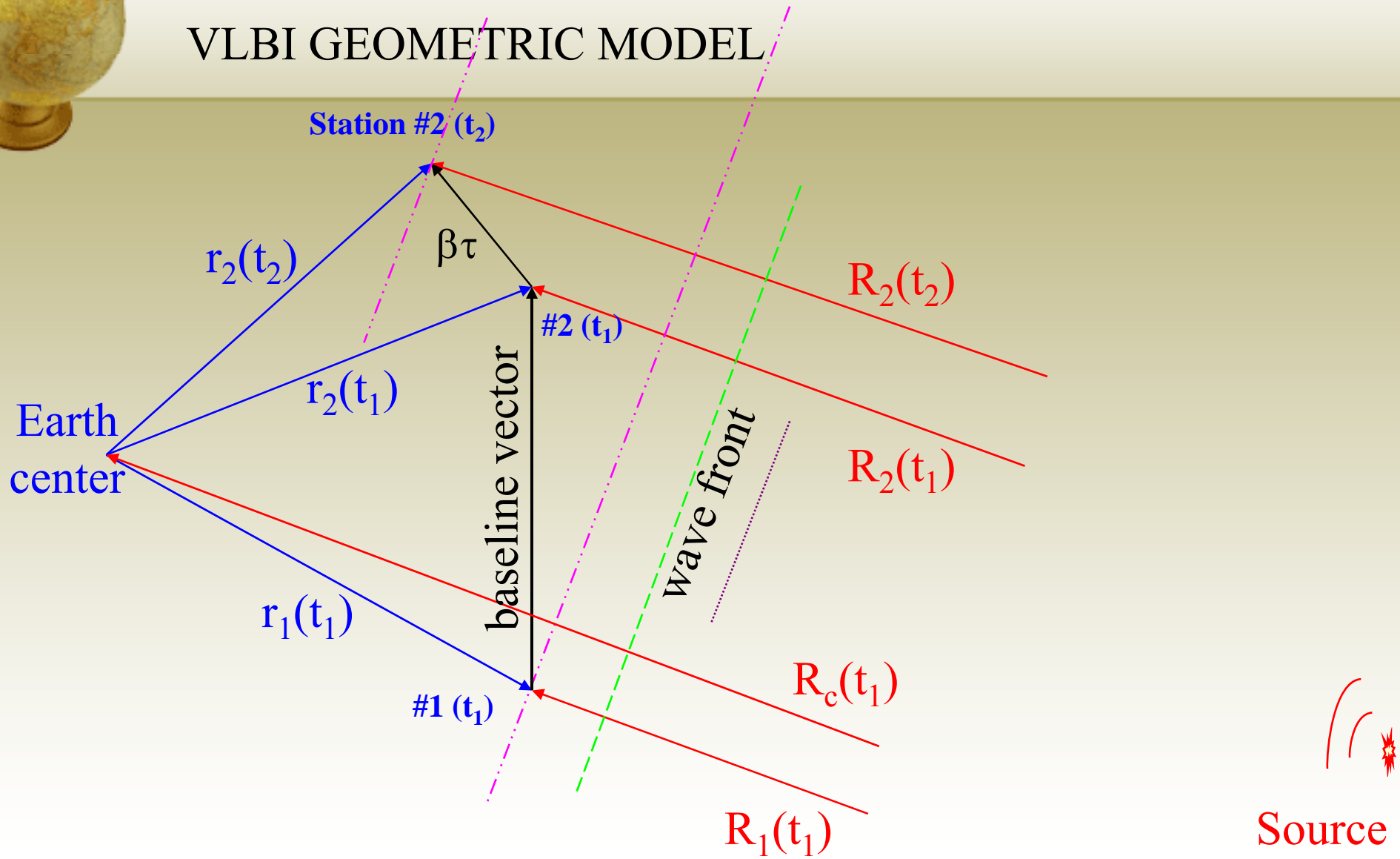


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Thank You ...



VLBI GEOMETRIC MODEL



$$c\tau = c(t_2 - t_1) = |\mathbf{R}_c(t_1) + \mathbf{r}_2(t_1) + \beta\tau| - |\mathbf{R}_c(t_1) + \mathbf{r}_1(t_1)|$$