## What makes a community?

#### mutuality of ties

everybody in the group knows everybody else

 frequency of ties among members
everybody in the group has links to at least k others in the group

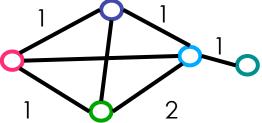
closeness or reachability of subgroup members

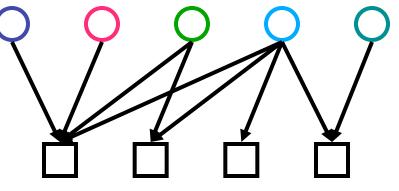
individuals are separated by at most n hops

relative frequency of ties among subgroup members compared to nonmembers

## Affiliation networks

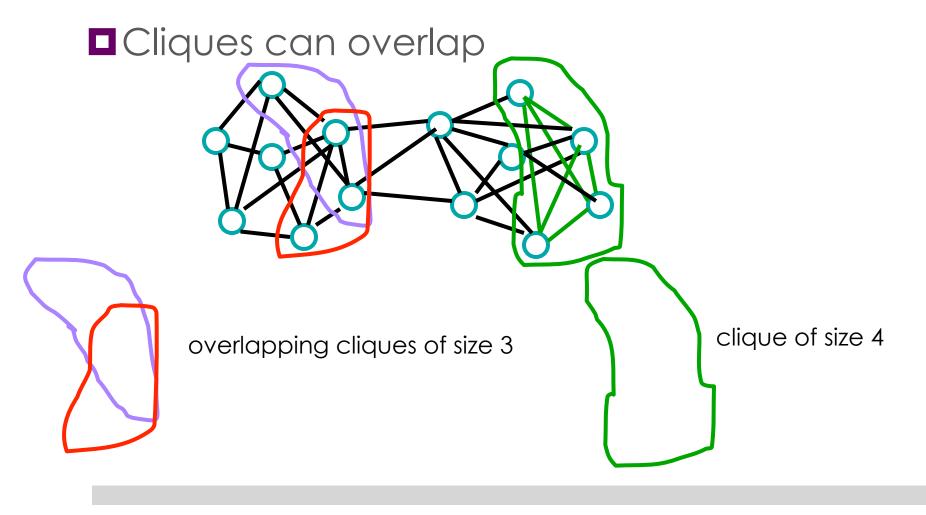
otherwise known as
membership network
e.g. board of directors
hypernetwork or hypergraph
bipartite graphs
interlocks





# Cliques

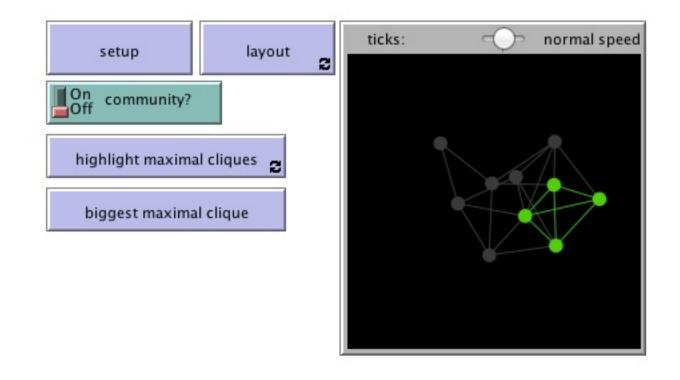
### Every member of the group has links to every other member



## Cliques betray community structure

Go to <u>http://www.ladamic.com/netlearn/nw/Cliques.html</u>

Try the ER vs. community structure setup (they are the same as for the opinion formation model)



# Quiz question

Which has a larger maximal clique?
network with community structure
the equivalent ER random graph

## Meaningfulness of cliques

#### Not robust

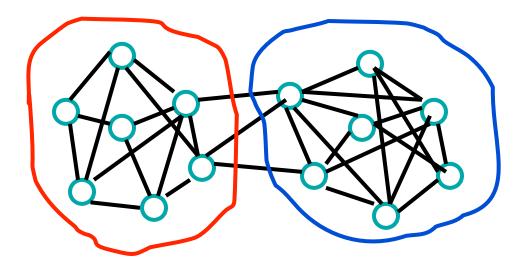
one missing link can disqualify a clique

Not interesting
everybody is connected to everybody else
no core-periphery structure
no centrality measures apply

How cliques overlap can be more interesting than that they exist

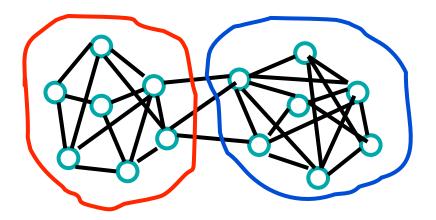
#### k-cores: similar idea, less stringent

Each node within a group is connected to k other nodes in the group



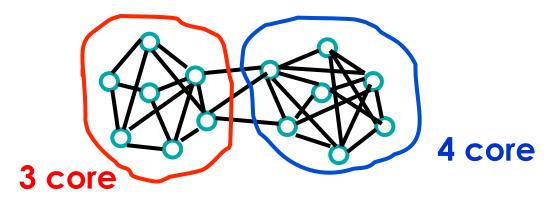
# Quiz Question

- What is the "k" for the core circled in red?
- What is the "k" for the core circled in blue?

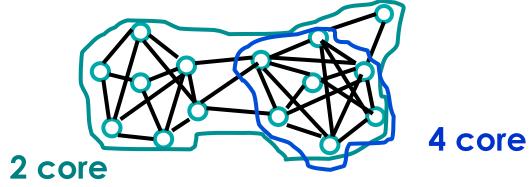


## k-cores

Each node within a group is connected to k other nodes in the group



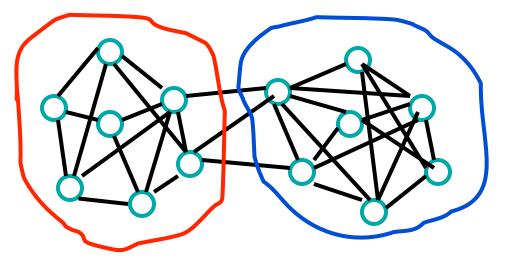
but even this is too stringent of a requirement for identifying natural communities



# subgroups based on reachability and diameter

#### n – cliques

maximal distance between any two nodes in subgroup is n



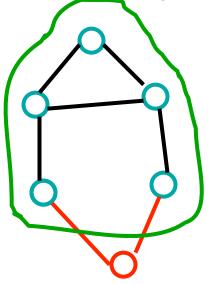
2-cliques

- theoretical justification
  - information flow through intermediaries

# considerations with n-cliques

#### problem

- diameter may be greater than n
- n-clique may be disconnected (paths go through nodes not in subgroup)



2 – clique diameter = 3

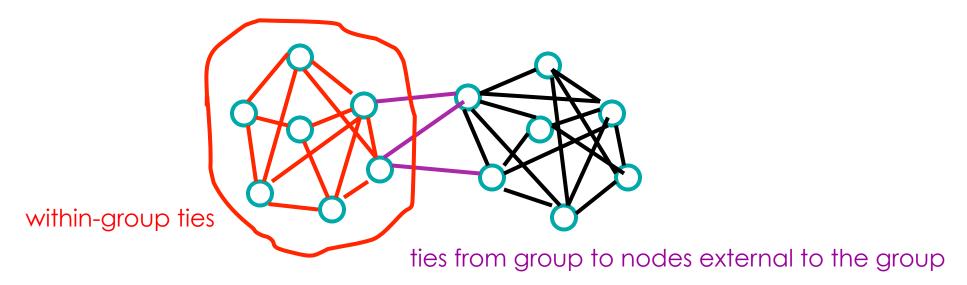
path outside the 2-clique

fix

n-club: maximal subgraph of diameter 2

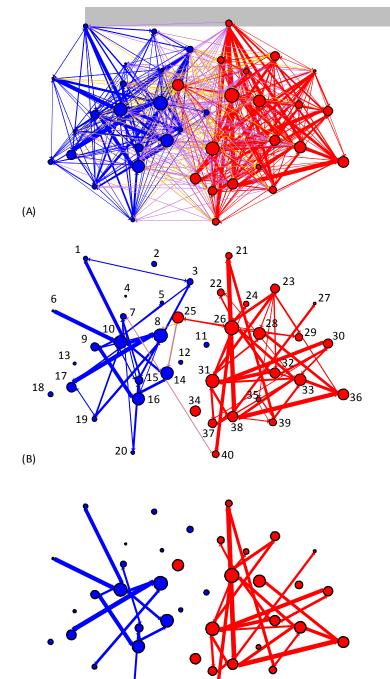
# p-cliques: frequency of in group ties

partition the network into clusters where vertices have at least a proportion p (number between 0 and 1) of neighbors inside the cluster.



# cohesion in directed & weighted networks

- something we've already learned how to do:
  - find strongly connected components
- keep only a subset of ties before finding connected components
  - reciprocal ties
  - edge weight above a threshold





39 Dean's World 40 Volokh Example: political blogs (Aug 29<sup>th</sup> – Nov 15<sup>th</sup>, 2004)

- A) all citations between Alist blogs in 2 months preceding the 2004 election
- B) citations between A-list blogs with at least 5 citations in both directions
- C) edges further limited to those exceeding 25 combined citations

only 15% of the citations bridge communities

source: Adamic & Glance, LinkKDD200