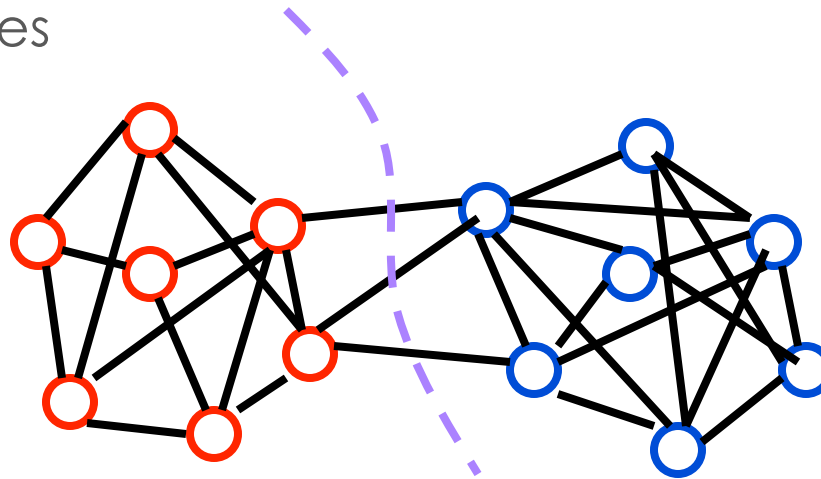


Community finding vs. other approaches

- Social and other networks have a natural community structure
- We want to discover this structure rather than impose a certain size of community or fix the number of communities

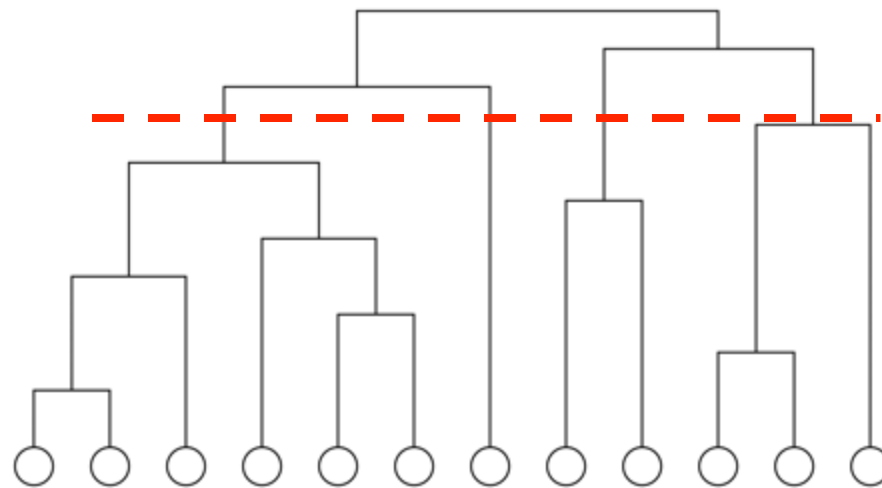


- Without “looking”, can we discover community structure in an automated way?

Hierarchical clustering

■ Process:

- after calculating the “distances” for all pairs of vertices
- start with all n vertices disconnected
- add edges between pairs one by one in order of decreasing weight
- result: nested components, where one can take a ‘slice’ at any level of the tree

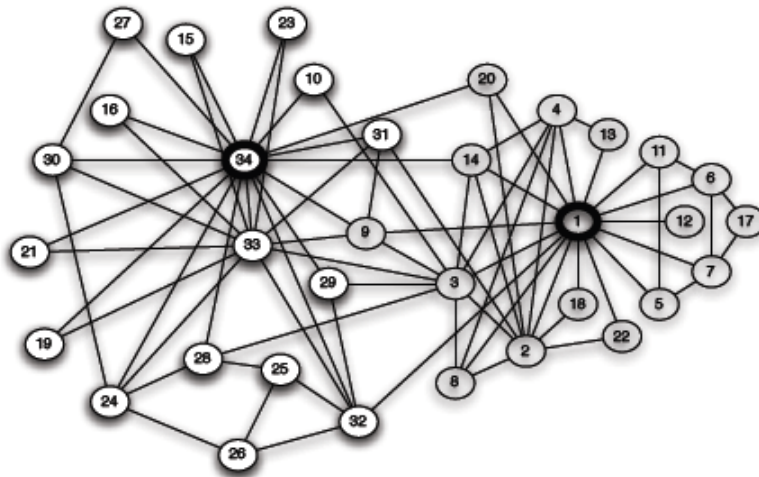


Hierarchical clustering

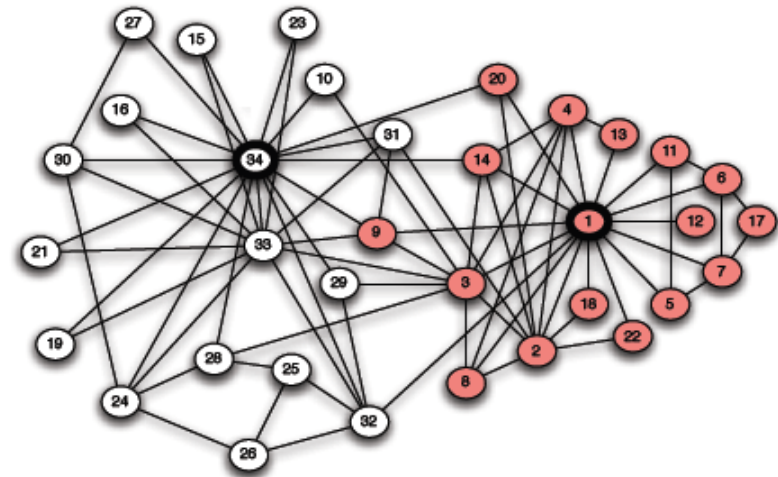
■ Process:

- after calculating the weights W for all pairs of vertices
- start with all n vertices disconnected
- add edges between pairs one by one in order of decreasing weight
- Efficient and successful implementation in Pajek...

Zachary Karate Club



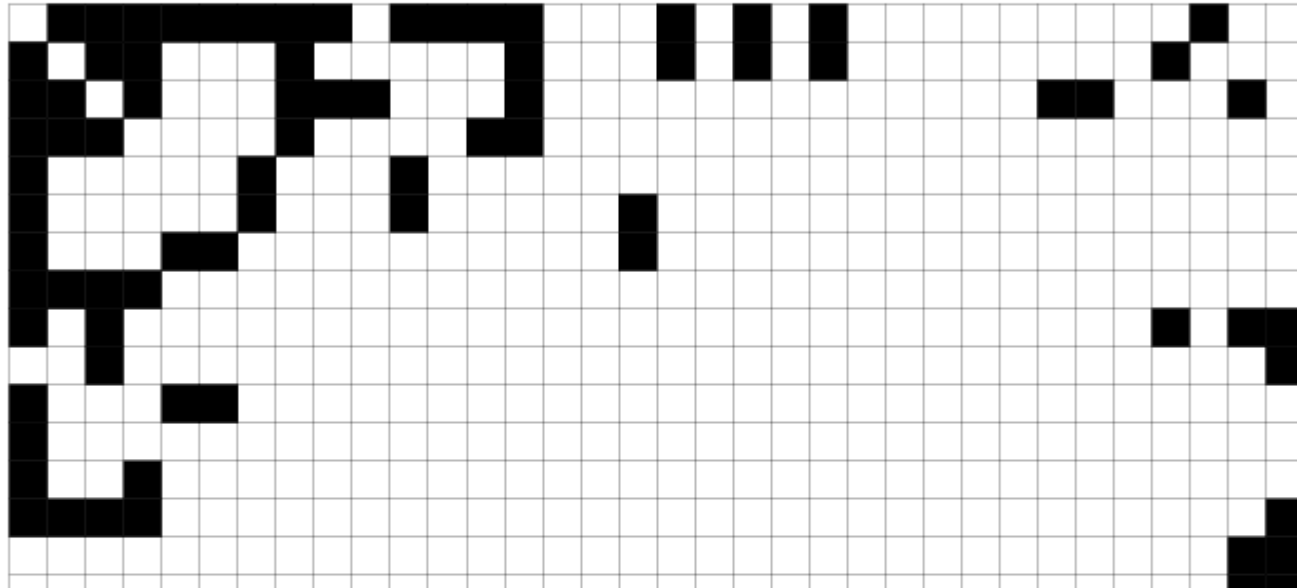
(a) *Karate club network*



(b) *After a split into two clubs*

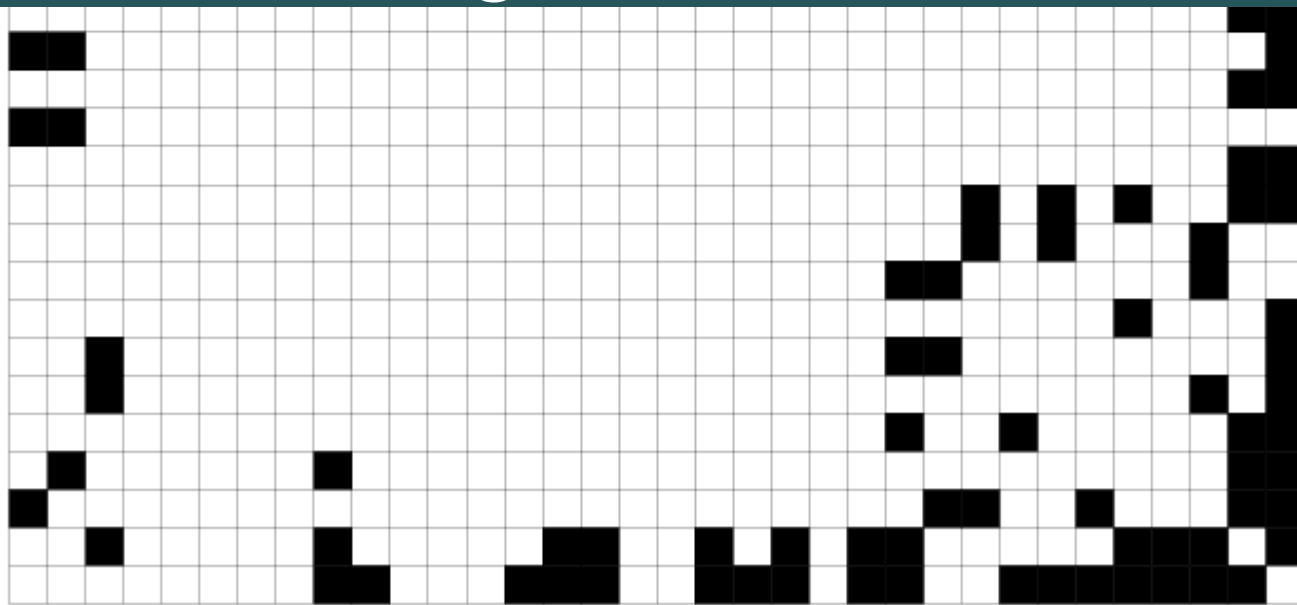
source:Easley/Kleinberg

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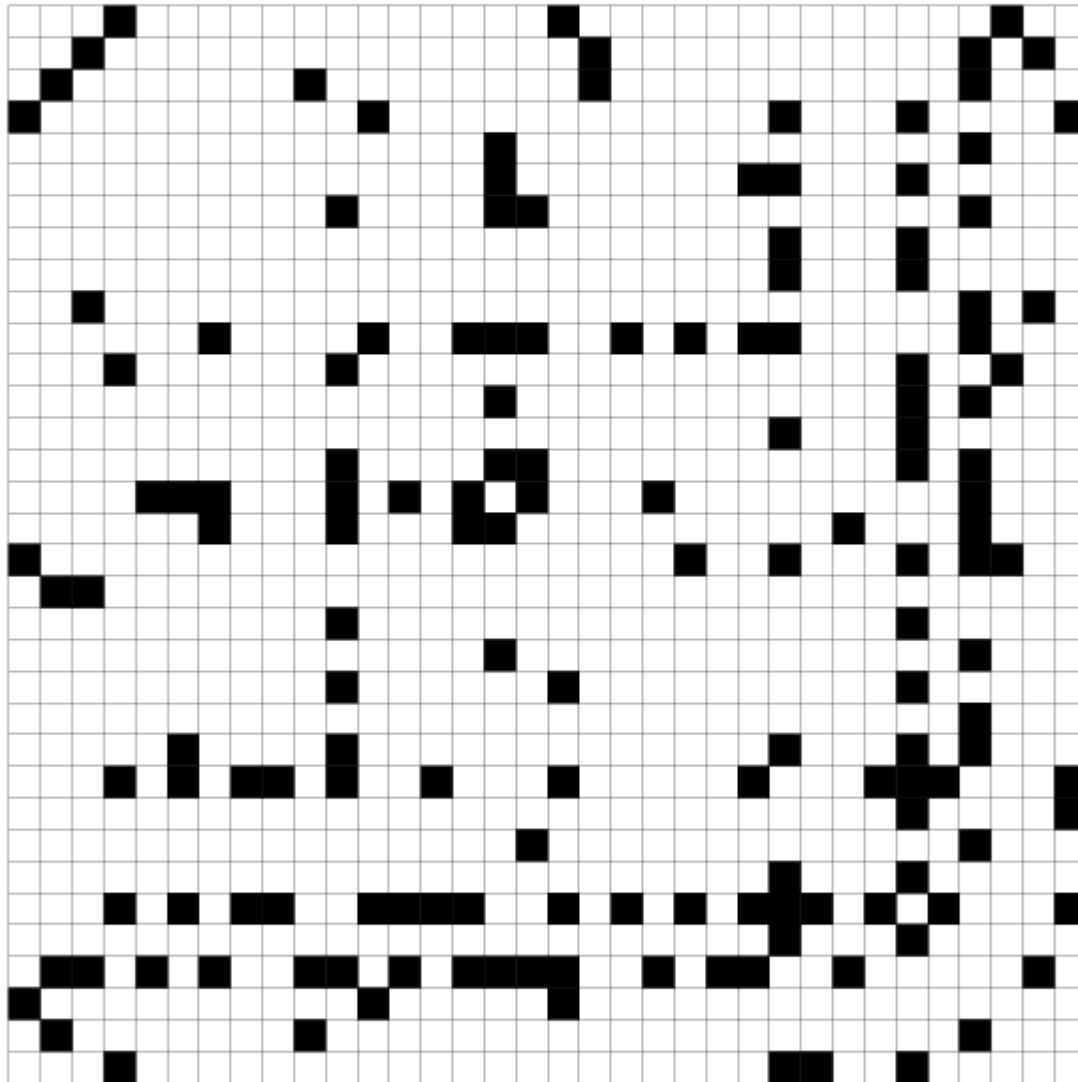
original matrix

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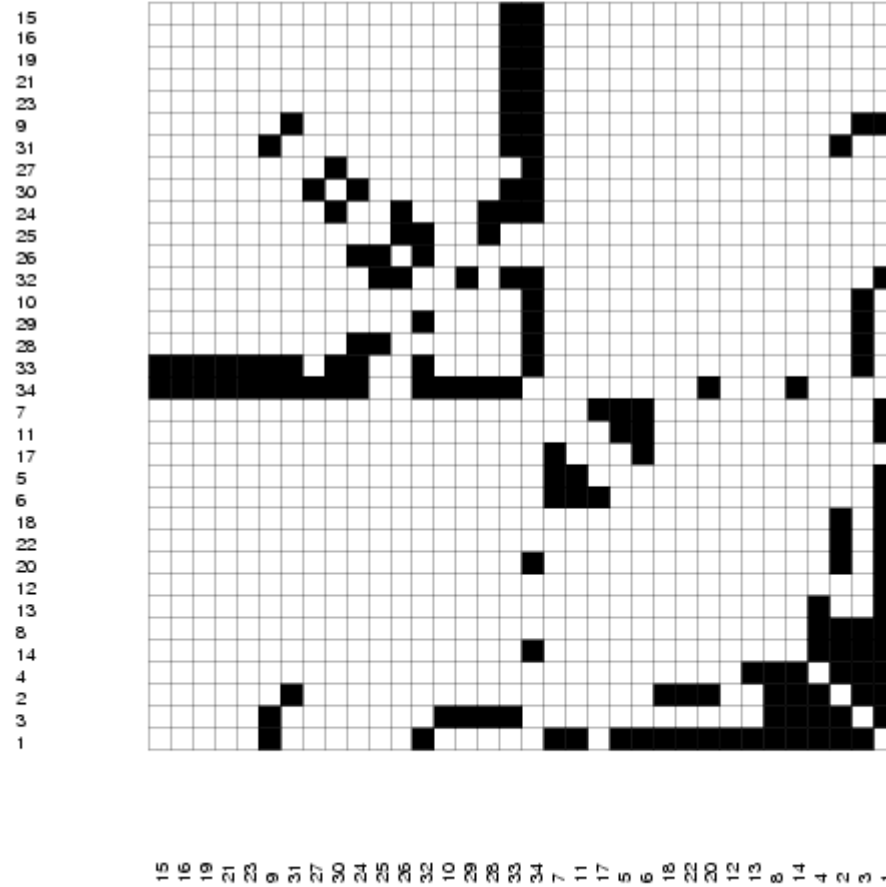


randomized karate club matrix

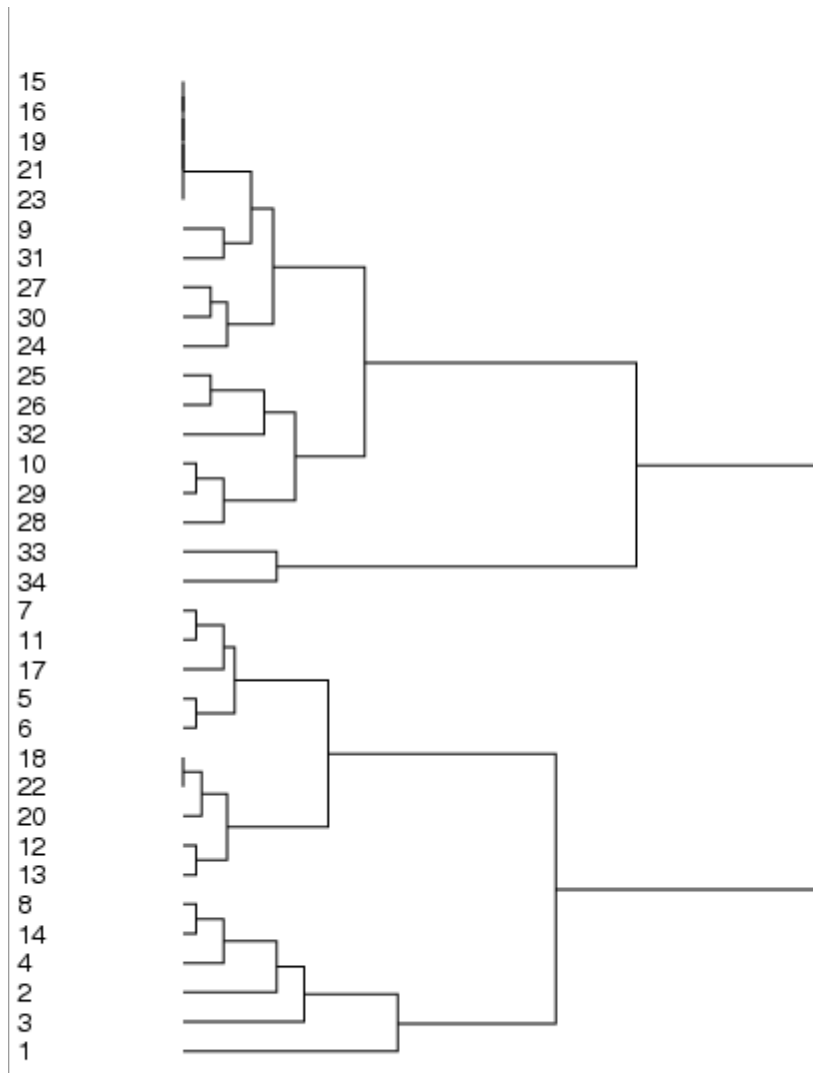
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permuted matrix



dendrogram



betweenness clustering

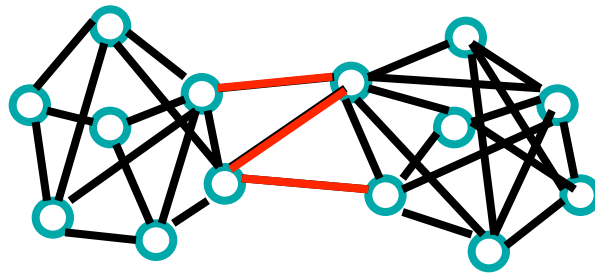
■ Algorithm

- compute the betweenness of all edges
- while (betweenness of any edge > threshold):
 - remove edge with highest betweenness
 - recalculate betweenness

■ Betweenness needs to be recalculated at each step

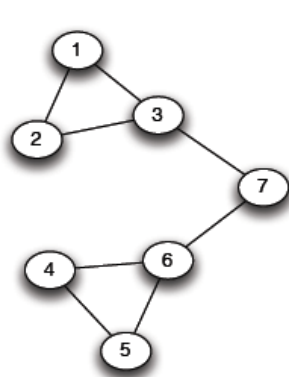
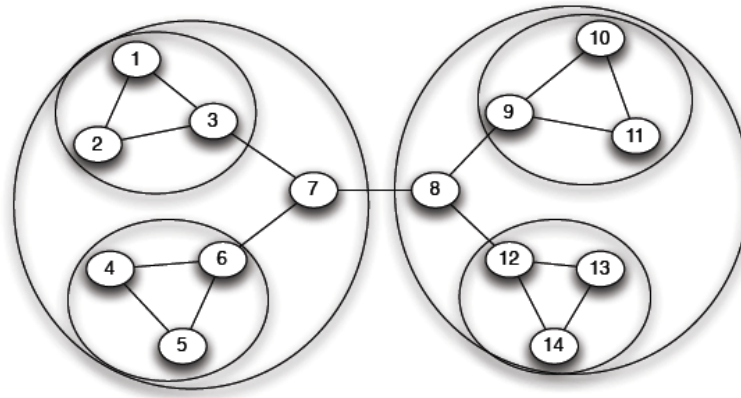
- removal of an edge can impact the betweenness of another edge
- very expensive: all pairs shortest path – $O(N^3)$
- may need to repeat up to N times
- does not scale to more than a few hundred nodes, even with the fastest algorithms

betweenness clustering algorithm

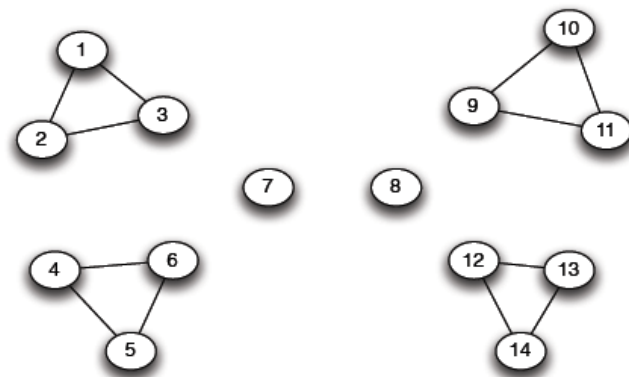


betweenness clustering:

- successively remove edges of highest betweenness (the bridges, or local bridges), breaking up the network into separate components

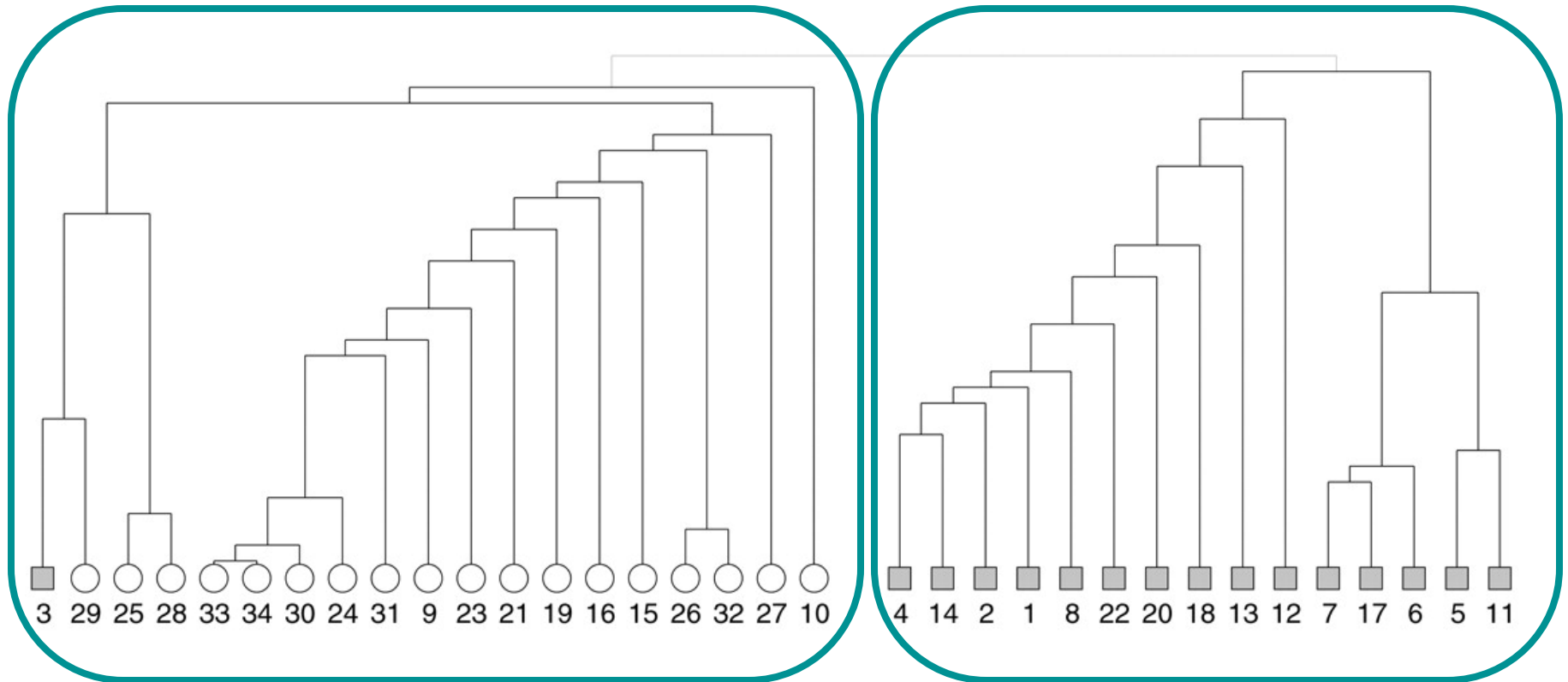


(a) Step 1



(b) Step 2

betweenness clustering algorithm & the karate club data set



source: Girvan and Newman, PNAS June 11, 2002 99(12):7821-7826

Modularity

- Consider edges that fall within a community or between a community and the rest of the network
- Define modularity:

$$Q = \frac{1}{2m} \sum_{vw} \left[A_{vw} - \frac{k_v k_w}{2m} \right] \delta(c_v, c_w)$$

if vertices are in the same community

adjacency matrix

probability of an edge between two vertices is proportional to their degrees

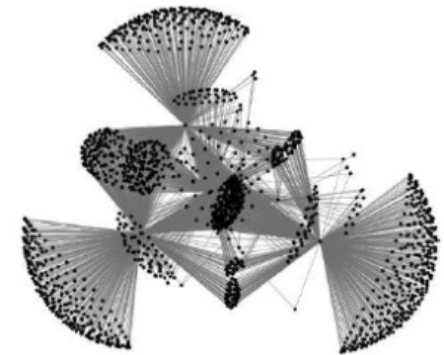
- For a random network, $Q = 0$
 - the number of edges within a community is no different from what you would expect

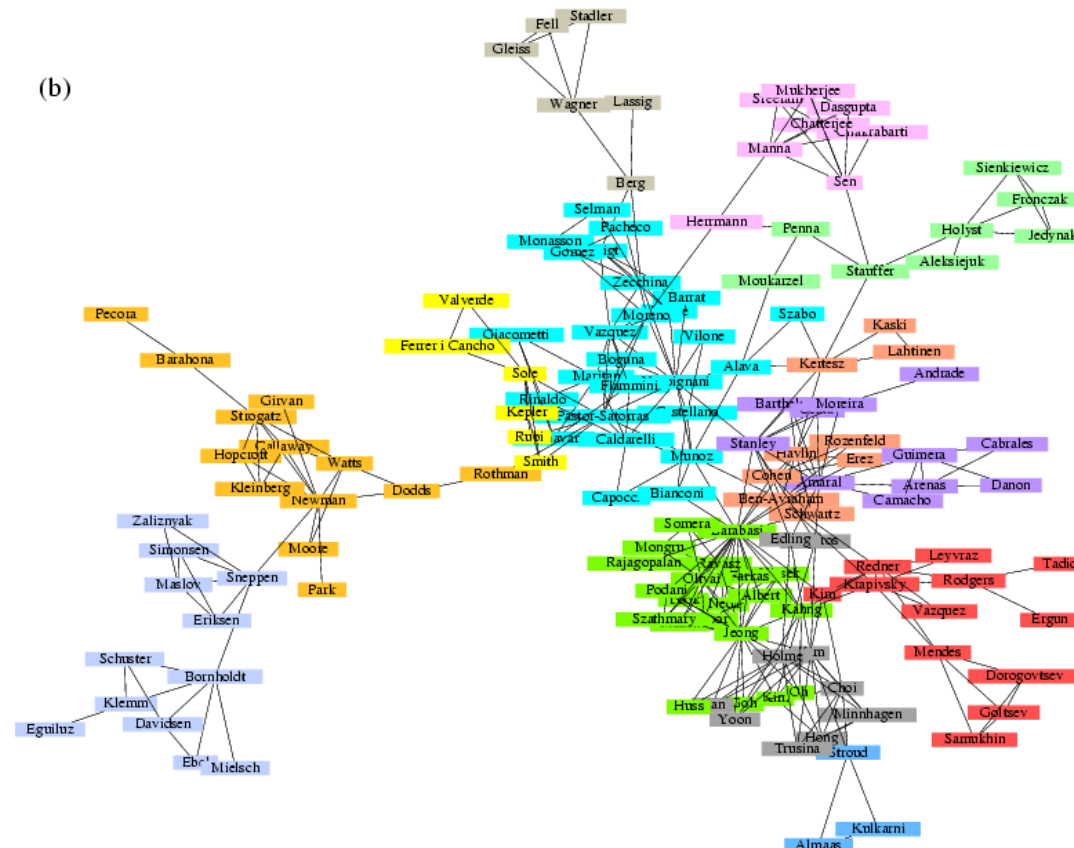
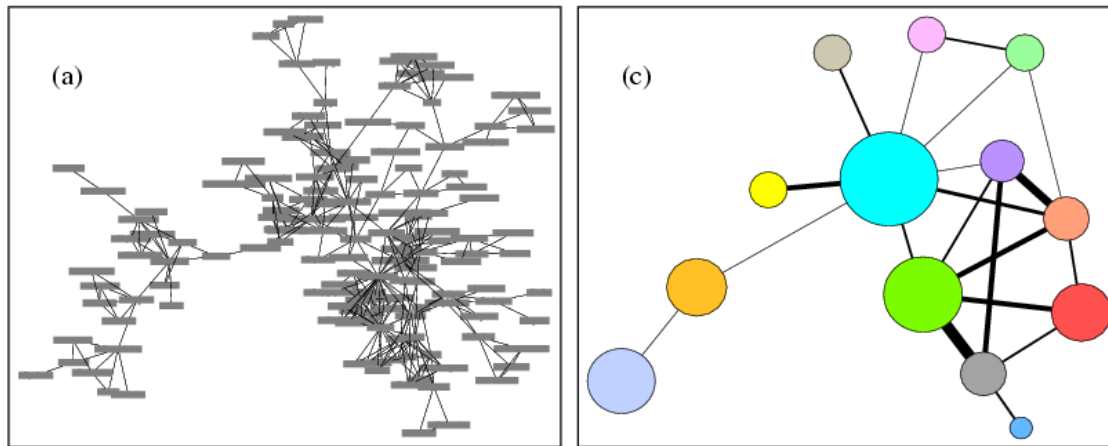
Finding community structure in very large networks

Authors: [Aaron Clauset](#), [M. E. J. Newman](#), [Cristopher Moore](#) 2004

Modularity

- Algorithm
 - start with all vertices as isolates
 - follow a greedy strategy:
 - successively join clusters with the greatest increase ΔQ in modularity
 - stop when the maximum possible $\Delta Q \leq 0$ from joining any two
 - successfully used to find community structure in a graph with $> 400,000$ nodes with > 2 million edges
 - Amazon's people who bought this also bought that...
 - alternatives to achieving optimum ΔQ :
 - simulated annealing rather than gre





**Reminder of
how
modularity
can help us
visualize large
networks**

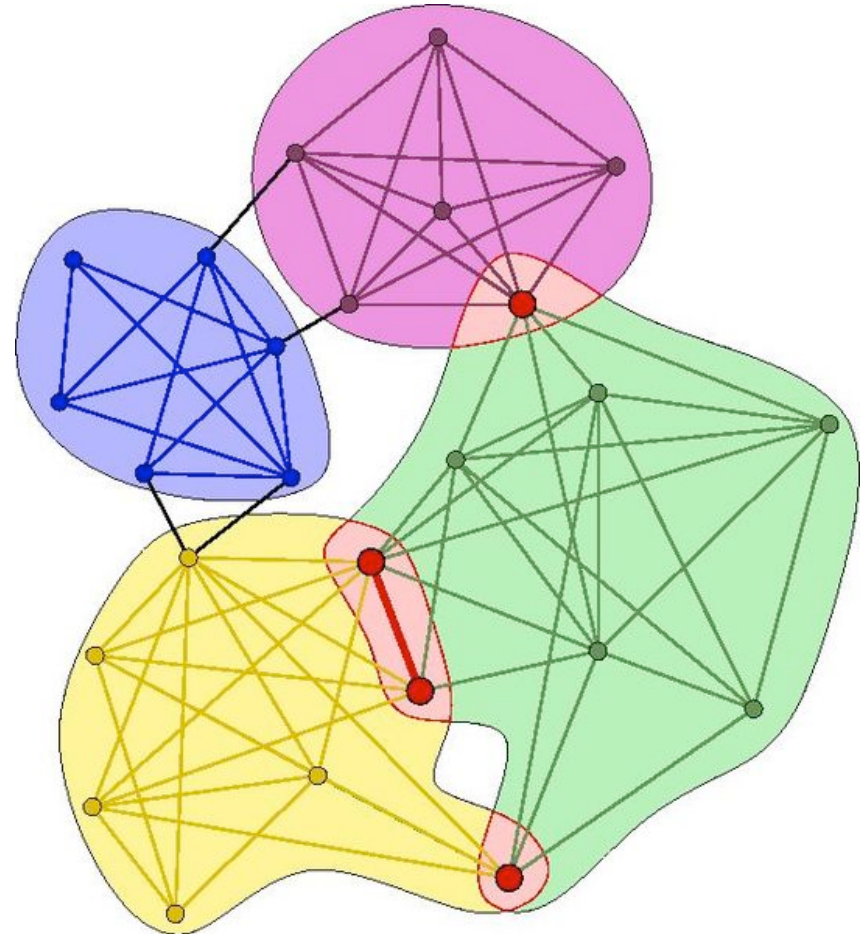
What if communities overlap?

- Recent research has found that for communities such as Orkut and Flickr, community finding algorithms cannot identify communities of more than ~100 nodes
- Statistical Properties of Community Structure in Large Social and Information Networks by J. Leskovec, K. Lang, A. Dasgupta, M. Mahoney. *International World Wide Web Conference (WWW)*, 2008. [[Video](#)]

Clique finder

■ <http://cfinder.org>

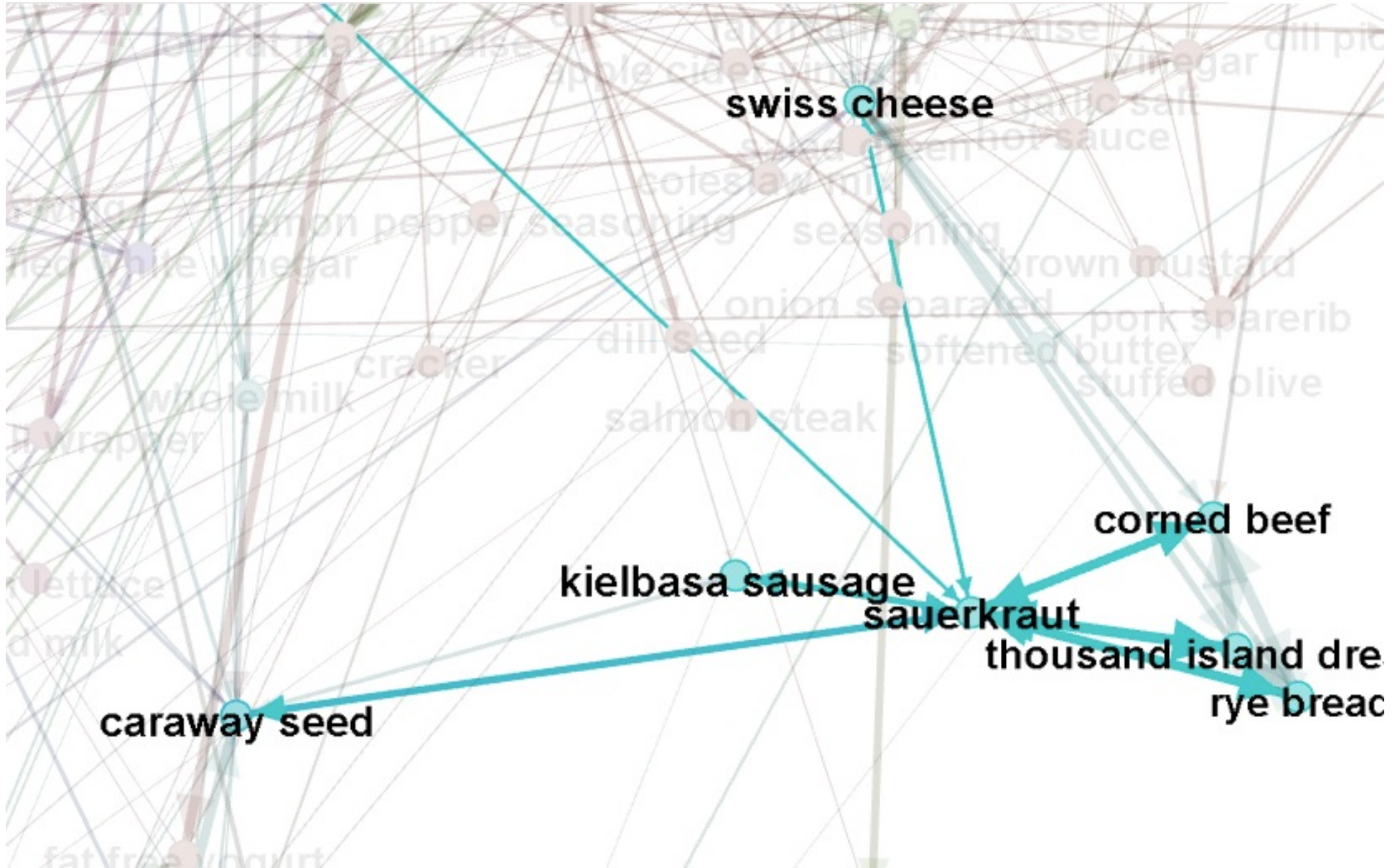
Uncovering the overlapping community structure of complex networks in nature and society G. Palla, I. Derényi, I. Farkas, and T. Vicsek:
Nature 435, 814–818 (2005)



wrap up

- ▣ community structure is a way of ‘x-raying’ the network, finding out what it’s made of
- ▣ you can look for specific structures
 - ▣ k-cliques, k-cores, etc.
- ▣ but most popular is to discover the “natural” community boundaries

For your assignment: community finding
& ingredients 😊



An information theoretic approach

- How to most concisely describe a random walk on the network using huffman codes? Prefixes become communities...



<http://www.pnas.org/content/105/4/1118>

<http://www.mapequation.org/mapgenerator/index.html>