

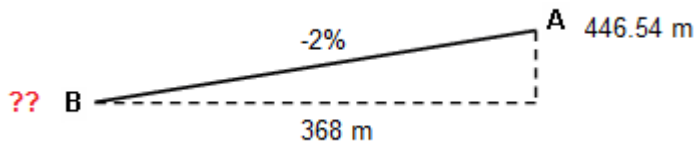
(10 p) 1. A horizontal distance was recorded as 242.84 m with a 20-m tape that was 20.003 m under standard conditions. Calculate the true horizontal distance.

SOLUTION :

Correction per tape length = -error = $-(20-20.003) = +0.003$ m
Tape correction = $(242.84/20)*0.003 = 0.036$ m
Corrected horizontal distance = $242.84+0.036 = \mathbf{242.876}$ m

(10 p) 2. Elevation of point A is 446.54 m and slope of line from point A to B is -2%. If the horizontal distance between the points A and B is 368 m, calculate the elevation of the point B.

SOLUTION :



Vertical distance = $368*(-0.02) = -7.36$ m (since point B is lower)
Elevation of Point B = $446.54 - 7.36 = \mathbf{439.18}$ m

(10 p) 3. Make the necessary conversions for the followings.

- a) $24^\circ = ?$ % (slope) b) $3\pi/7 = ?$ degree c) $130^\circ = ?$ radian d) $260 \text{ cm}^3 = ?$ dl (deciliter)

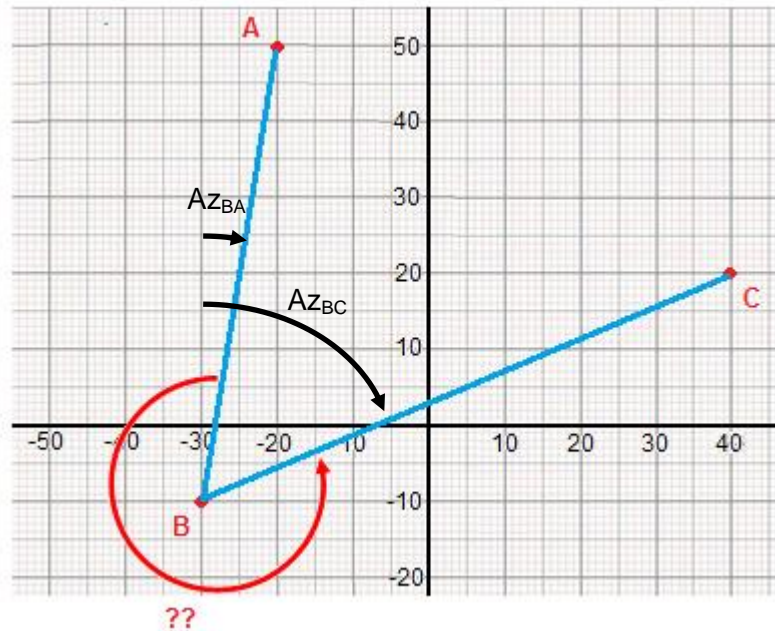
SOLUTION :

- a) $24^\circ = ?$ % (slope) $\tan 24^\circ = 0.445$ then slope = 44.5%
b) $3\pi/7 = ?$ degree $(3\pi/7)*360/2\pi = 77.1$ degree
c) $130^\circ = ?$ radian $130*2\pi/360=0.72\pi$ or 2.27 radian
d) $260 \text{ cm}^3 = ?$ dl (deciliter) $260/1000=0.26$ liter = 2.6 deciliter

(20 p) 4. The coordinates of the points ABC (a broken line) are given. Calculate the angle to the left at point B in degree unit. Use the azimuths of lines.

| Point | Coordinates (m) | |
|-------|-----------------|----------|
| | Easting | Northing |
| A | -20 | 50 |
| B | -30 | -10 |
| C | 40 | 20 |

SOLUTION :



Angle to the right at point B = $Az_{BC} - Az_{BA} + 360^\circ$

$$\alpha = \text{atan} [(E_A - E_B) / (N_A - N_B)] = \text{atan} [(-20 - (-30)) / (50 - (-10))] = \text{atan} (10/60) = 9.46^\circ$$

If both ΔE and ΔN are positive, then $Az_{BA} = 9.46^\circ$

$$\alpha = \text{atan} [(E_C - E_B) / (N_C - N_B)] = \text{atan} [(40 - (-30)) / (20 - (-10))] = \text{atan} (70/30) = 66.80^\circ$$

If both ΔE and ΔN are positive, then $Az_{BC} = 66.80^\circ$

Angle to the left at point B = $360^\circ - (66.80^\circ - 9.46^\circ) = 302.66^\circ$

(15 p) 5. Coordinates of points A and B are given as follows. Calculate the Azimuth and Bearing angles of the line AB in degree.

$$E_A = 160 \quad N_A = 210 \quad E_B = 80 \quad N_B = 40$$

SOLUTION :

$$\alpha = \text{atan} [(E_B - E_A) / (N_B - N_A)] = \text{atan} [(80 - 160) / (40 - 210)] = \text{atan} (-80/-170) = 25.20^\circ$$

If both ΔE and ΔN are negative, then $Az_{BA} = 180 + \alpha = 205.20^\circ$

$$\text{Bearing of AB} = Az_{BA} - 180 = S25.20^\circ W$$

(25 p) 6. If the following records are given for a path on the horizontal plane, calculate the horizontal distance between the points A and D.

Azimuth of AB is 136°

Length of line AB = 120 m

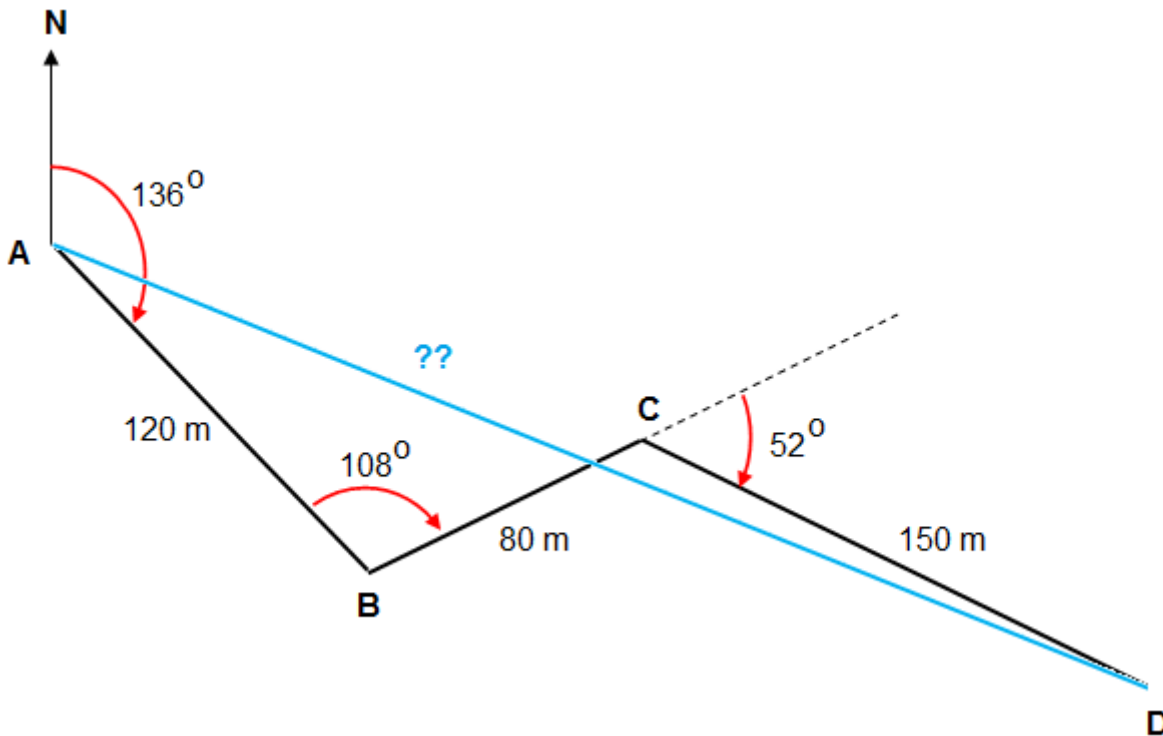
Angle to the right at point B is 108°

Length of line BC = 80 m

Deflection angle at point C 52° R

Length of line CD = 150 m

SOLUTION :



$$\text{Azimuth}_{BC} = \text{Az}_{AB} + 108 - 180 = 136 + 108 - 180 = 64^\circ$$

$$\text{Azimuth}_{CD} = \text{Az}_{BC} + 52 = 64 + 52 = 116^\circ$$

$$\Delta E \text{ of line AB} = 120 \cdot \sin 136 = 83.36 \text{ m}$$

$$\Delta N \text{ of line AB} = 120 \cdot \cos 136 = -86.32 \text{ m}$$

$$\Delta E \text{ of line BC} = 80 \cdot \sin 64 = 71.90 \text{ m}$$

$$\Delta N \text{ of line BC} = 80 \cdot \cos 64 = 35.07 \text{ m}$$

$$\Delta E \text{ of line CD} = 150 \cdot \sin 116 = 134.82 \text{ m}$$

$$\Delta N \text{ of line CD} = 150 \cdot \cos 116 = -65.76 \text{ m}$$

$$\text{Departure of Line AD} = \Delta E_{AB} + \Delta E_{BC} + \Delta E_{CD} = 83.36 + 71.90 + 134.82 = 290.08 \text{ m}$$

$$\text{Latitude of Line AD} = \Delta N_{AB} + \Delta N_{BC} + \Delta N_{CD} = -86.32 + 35.07 - 65.76 = -117.01 \text{ m}$$

$$\text{Distance AD} = (\Delta E^2 + \Delta N^2)^{1/2} = (290.08^2 + 117.01^2)^{1/2} = \mathbf{312.79 \text{ m}}$$

(10 p) 7. Convert the following bearings to azimuths.

a) S $3^\circ 38'$ W

b) N $64^\circ 24'$ W

c) S $82^\circ 19'$ E

d) N $45^\circ 27'$ E

SOLUTION :

$$\text{a) Azimuth} = 180 + 3^\circ 38' = 183^\circ 38' = 183.63^\circ$$

$$\text{b) Azimuth} = 360 - 64^\circ 24' = 295^\circ 36' = 295.60^\circ$$

$$\text{c) Azimuth} = 180 - 82^\circ 19' = 97^\circ 41' = 97.68^\circ$$

$$\text{d) Azimuth} = 45^\circ 27' = 45.45^\circ$$