



HAB 619 Introduction to Scientific Computing in Sports Science

#5

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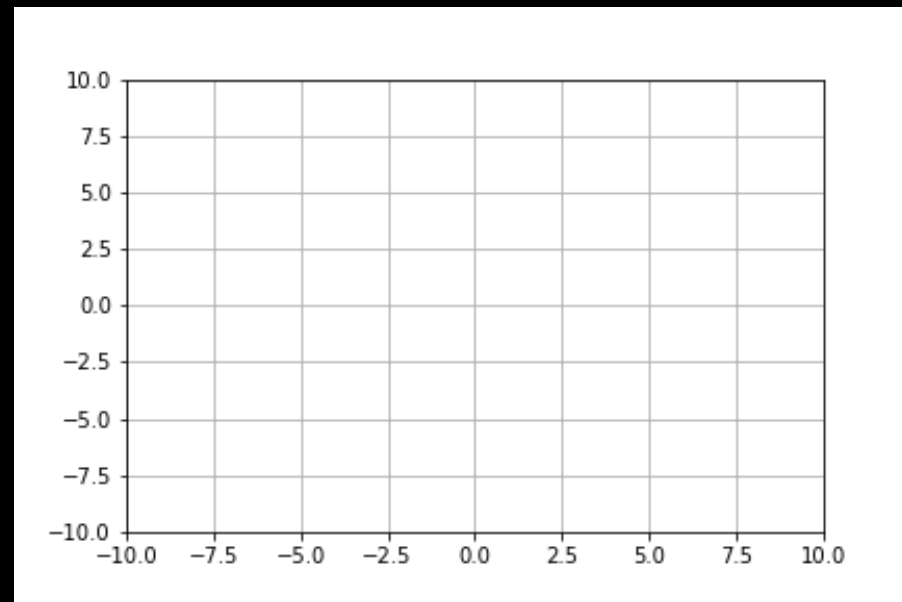
Establishing the Size of the Plotting Area

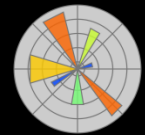
```
import numpy as np
import matplotlib.pyplot as plt

x1=-10
x2=10
y1=-10
y2=10
plt.axis([x1,x2,y1,y2])

plt.axis('on')
plt.grid(True)

plt.show()
```



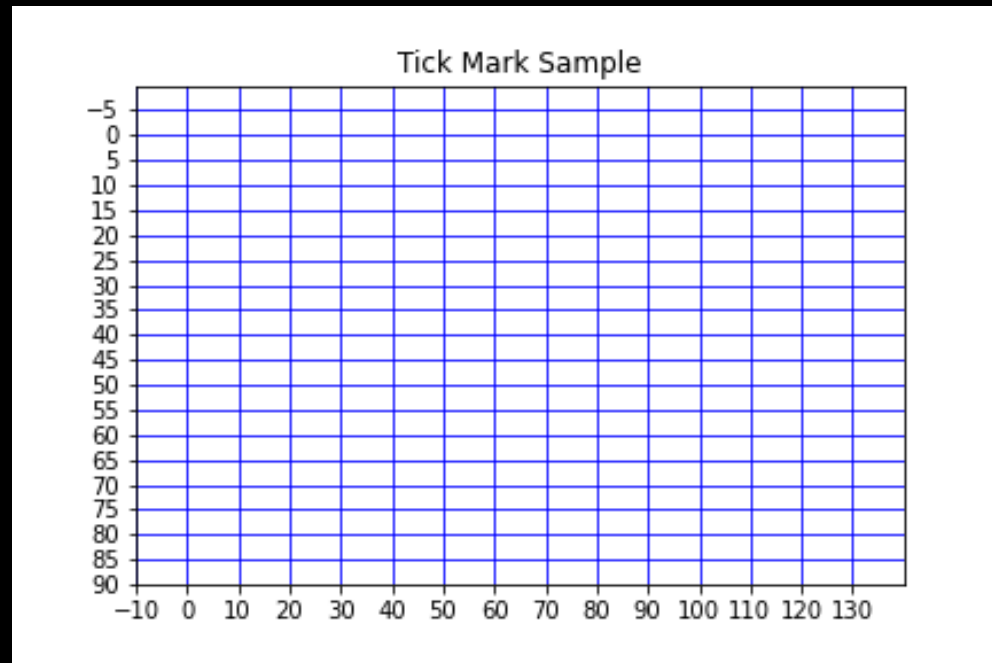


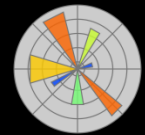
Tick Marks

```
import numpy as np
import matplotlib.pyplot as plt

x1 = -10
x2 = 140
y1 = 90
y2 = -10
plt.axis([x1,x2,y1,y2])
plt.axis('on')
plt.grid(True, color='b')
plt.title('Tick Mark Sample')
xmin = x1
xmax = x2
dx = 10
ymin = y1
ymax = y2
dy = -5
plt.xticks(np.arange(xmin, xmax, dx))
plt.yticks(np.arange(ymin, ymax, dy))

plt.show()
```





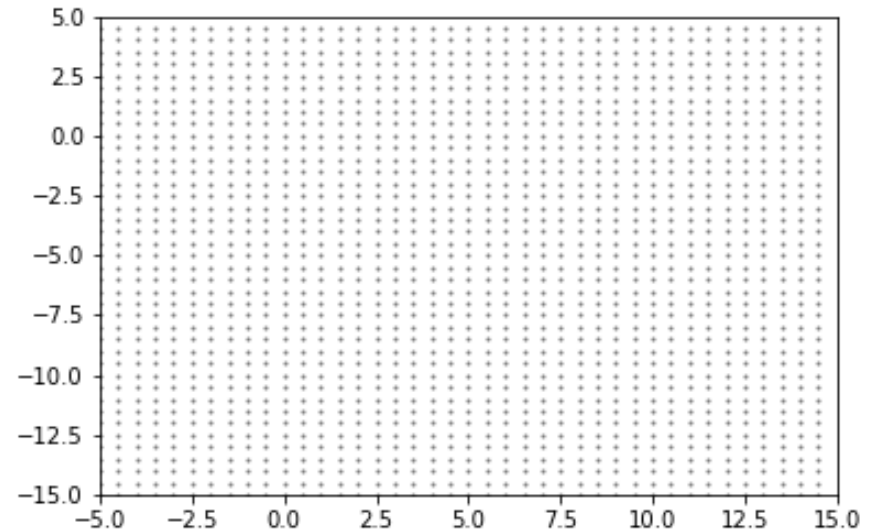
```
import numpy as np
import matplotlib.pyplot as plt
```

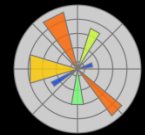
```
x1=-5
x2=15
y1=-15
y2=5
plt.axis([x1,x2,y1,y2])
plt.axis('on')
```

```
dx=.5 #x spacing
dy=.5 #y spacing
for x in np.arange(x1,x2,dx) :
    for y in np.arange(y1,y2,dy): #y locations
        plt.scatter(x,y,s=1,color='grey') #plot a grey point at x,y

plt.show()
```

Tick Marks





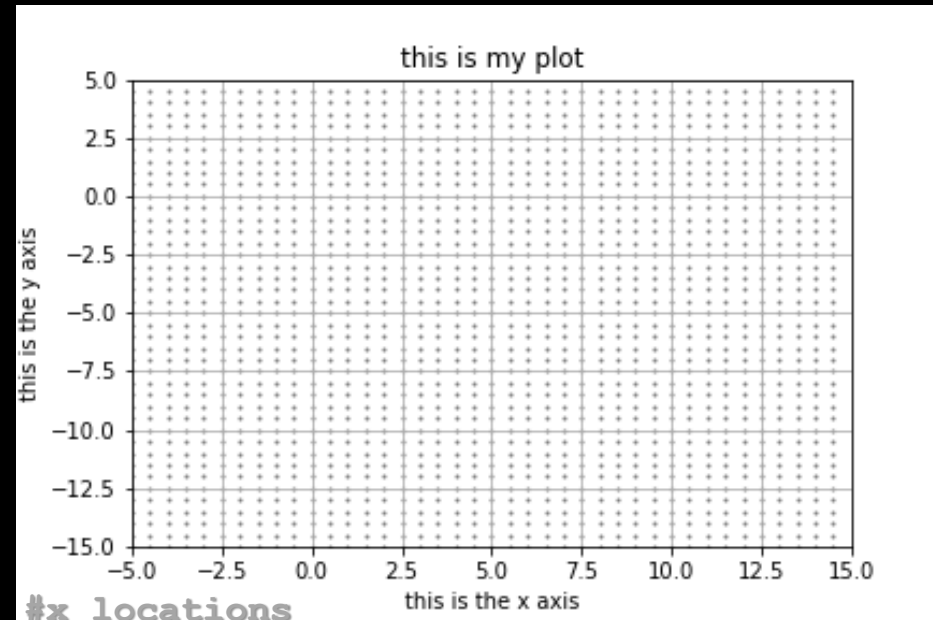
Plot Title and Labelling the Axes

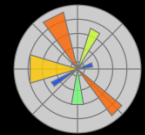
```
import numpy as np
import matplotlib.pyplot as plt
```

```
x1=-5
x2=15
y1=-15
y2=5
plt.axis([x1,x2,y1,y2])
plt.axis('on')
dx=.5 #x spacing
dy=.5 #y spacing
for x in np.arange(x1,x2,dx):
    for y in np.arange(y1,y2,dy): #y locations
        plt.scatter(x,y,s=1,color='grey') #plot a grey point at x,y

plt.grid(True)
plt.xlabel('this is the x axis')
plt.ylabel('this is the y axis')
plt.title('this is my plot')

plt.show()
```





Color

'k' for black

'b' for blue

'c' for cyan

'g' for green

'm' for magenta

'r' for red

'y' for yellow

'gray' or 'grey'

'lightgray' or 'lightgrey'

For example, the following statement will plot a green dot at coordinates x,y:

```
plt.scatter(x, y, color = 'g')
```



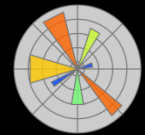

NumPy



Color

https://matplotlib.org/examples/color/named_colors.html

black	k	dimgray	dimgray
gray	grey	darkgray	darkgrey
silver	lightgray	lightgray	gainsboro
whitesmoke	w	white	snow
rosybrown	lightcoral	indianred	brown
firebrick	maroon	darkred	r
red	mistyrose	salmon	tomato
darksalmon	coral	orangered	lightsalmon
sienna	seashell	chocolate	saddlebrown
sandybrown	peachpuff	peru	linen
bisque	darkorange	burlywood	antiquewhite
tan	navajowhite	blanchedalmond	papayawhip
moccasin	orange	wheat	oldlace
floralwhite	darkgoldenrod	goldenrod	cornsilk
gold	lemonchiffon	khaki	palegoldenrod
darkkhaki	ivory	beige	lightyellow
lightgoldenrodyellow	olive	y	yellow
olivedrab	yellowgreen	darkolivegreen	greenyellow
chartreuse	lawngreen	honeydew	darkseagreen
palegreen	lightgreen	forestgreen	limegreen
darkgreen	g	green	lime
seagreen	mediumseagreen	springgreen	mintcream
mediumspringgreen	mediumaquamarine	aquamarine	turquoise
lightseagreen	mediumturquoise	azure	lightcyan
paleturquoise	darkslategray	darkslategrey	teal
darkcyan	c	aqua	cyan
darkturquoise	cadetblue	powderblue	lightblue
deepskyblue	skyblue	lightskyblue	steelblue
aliceblue	dodgerblue	lightslategray	lightslategray
slategray	slategrey	lightsteelblue	cornflowerblue
royalblue	ghostwhite	lavender	midnightblue
navy	darkblue	mediumblue	b
blue	slateblue	darkslateblue	mediumslateblue
mediumpurple	rebeccapurple	blueviolet	indigo
darkorchid	darkviolet	mediumorchid	thistle
plum	violet	purple	darkmagenta
m	fuchsia	magenta	orchid
mediumvioletred	deeppink	hotpink	lavenderblush
palevioletred	crimson	pink	lightpink



Color

https://matplotlib.org/examples/color/named_colors.html

```
"""
=====
Visualizing named colors
=====

Simple plot example with the named colors and its visual representation.
"""

from __future__ import division

import matplotlib.pyplot as plt
from matplotlib import colors as mcolors

colors = dict(mcolors.BASE_COLORS, **mcolors.CSS4_COLORS)

# Sort colors by hue, saturation, value and name.
by_hsv = sorted((tuple(mcolors.rgb_to_hsv(mcolors.to_rgba(color)[:3])), name)
                 for name, color in colors.items())
sorted_names = [name for hsv, name in by_hsv]
.....
.....
ax.set_xlim(0, X)
ax.set_ylim(0, Y)
ax.set_axis_off()

fig.subplots_adjust(left=0, right=1,
                    top=1, bottom=0,
                    hspace=0, wspace=0)

plt.show()
```




Color Mixing

You can mix your own hues from the primary colors of **red (r)**, **green (g)**, and **blue (b)** with the specification `color=(r,g,b)` where `r,g,b` are the values of red, green, and blue in the mix, with values of each ranging from 0 to 1.

```
import numpy as np
import matplotlib.pyplot as plt
```

```
plt.axis([0,100,0,10])
```

```
for x in np.arange(1,100,1):
```

```
    r=x/100
```

```
    g=0
```

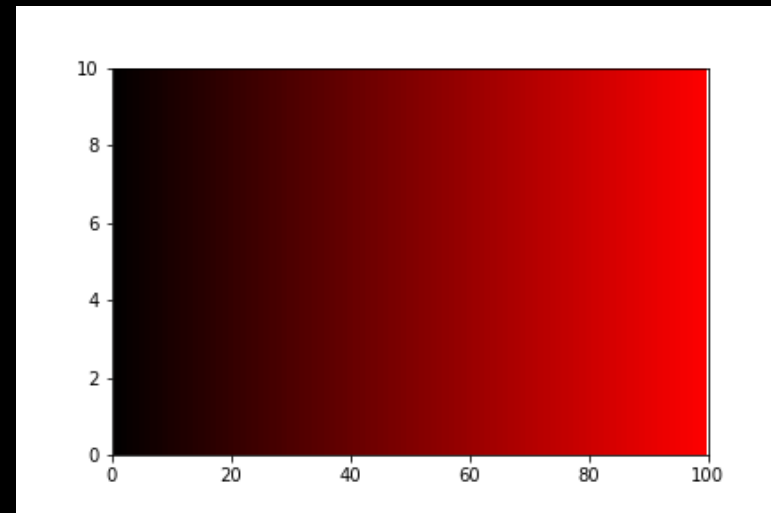
```
    b=0
```

```
    plt.plot([x,x],[0,10],linewidth=5,color=(r,g,b))
```

```
plt.show()
```

```
# r = x/100, g = 0, b = x/100
```

```
# r = x/100, g = x/100, b = 0
```





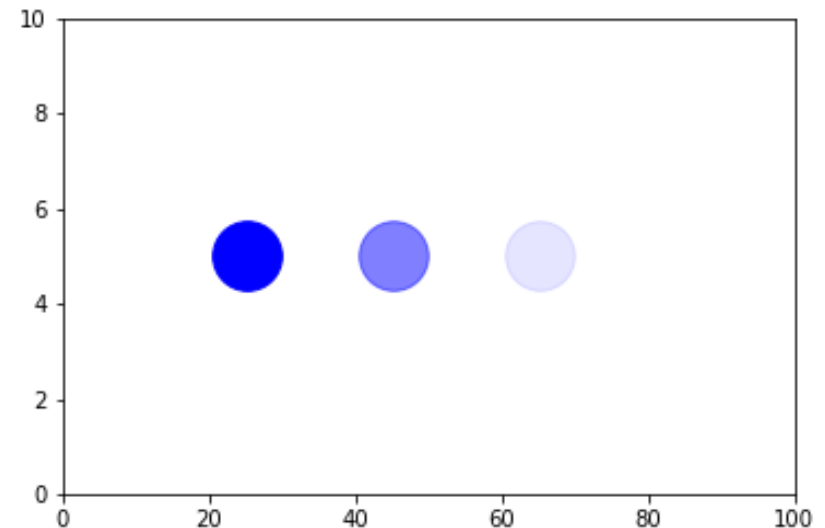
```
import numpy as np  
import matplotlib.pyplot as plt
```

```
plt.axis([0,100,0,10])
```

```
plt.scatter(25, 5, s=1000, color='b', alpha=1)  
plt.scatter(45, 5, s=1000, color='b', alpha=.5)  
plt.scatter(65, 5, s=1000, color='b', alpha=.1)
```

```
plt.show()
```

Color Intensity

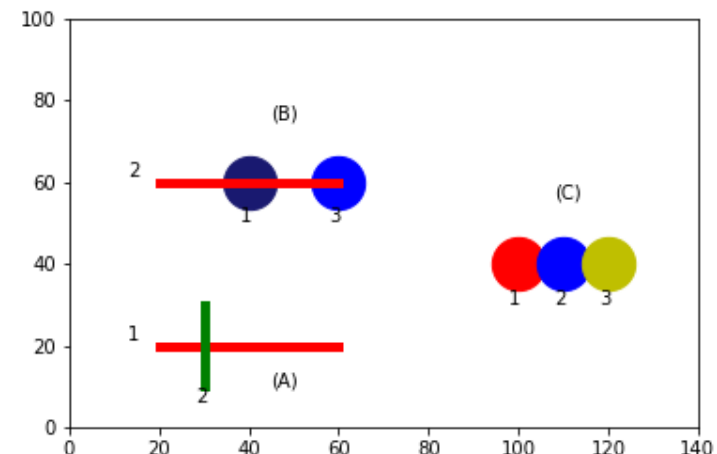




Overplotting

```
import numpy as np
import matplotlib.pyplot as plt
plt.axis([0,140,0,100])
#----- A
plt.text(45,10,'(A)')
plt.plot([20,60],[20,20],linewidth=5,color='r')
plt.text(13,21,'1')
plt.plot([30,30],[10,30],linewidth=5,color='g')
plt.text(28,6,'2')
#----- B
plt.text(45,75,'(B)')
plt.scatter(40,60,s=800,color='midnightblue')
plt.text(38,50,'1')
plt.plot([20,60],[60,60],linewidth=5,color='r')
plt.text(13,61,'2')
plt.scatter(60,60,s=800,color='b')
plt.text(58,50,'3')
#----- C
plt.text(108,56,'(C)')
plt.scatter(100,40,s=800,color='r')
plt.text(98,30,'1')
plt.scatter(110,40,s=800,color='b')
plt.text(108,30,'2')
plt.scatter(120,40,s=800,color='y')
plt.text(118,30,'3')

plt.show()
```





Lines Using plot()

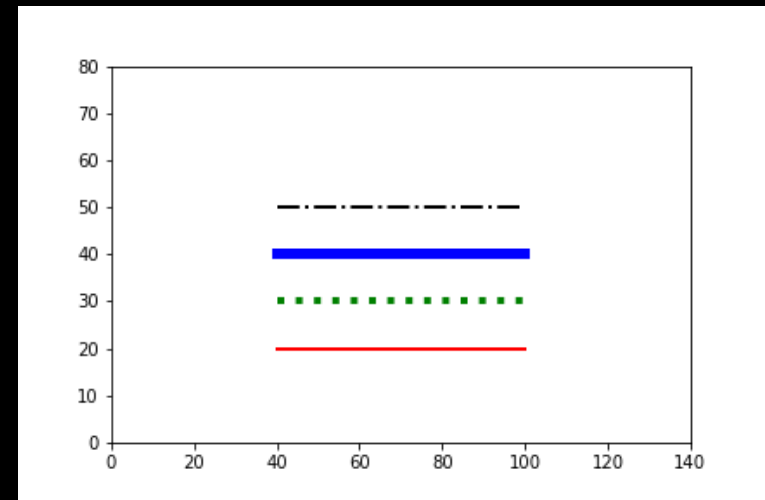
`plt.plot([x1,x2],[y1,y2],linewidth=linewidth, color='color', linestyle='linestyle')`
This command draws a line from x_1, y_1 to x_2, y_2 . It has a width specified by `linewidth`, a color by `color`, and a style by `linestyle`.

```
import numpy as np
import matplotlib.pyplot as plt
```

```
plt.axis([0,140,0,80])
```

```
plt.plot([40,100], [20,20], linewidth=2, color='r')
plt.plot([40,100], [30,30], linewidth=4, color='g', linestyle= ':')
plt.plot([40,100], [40,40], linewidth=6, color='b', linestyle= '-')
plt.plot([40,100], [50,50], linewidth=2, color='k', linestyle= '-.')
```

```
plt.show()
```





Arrows

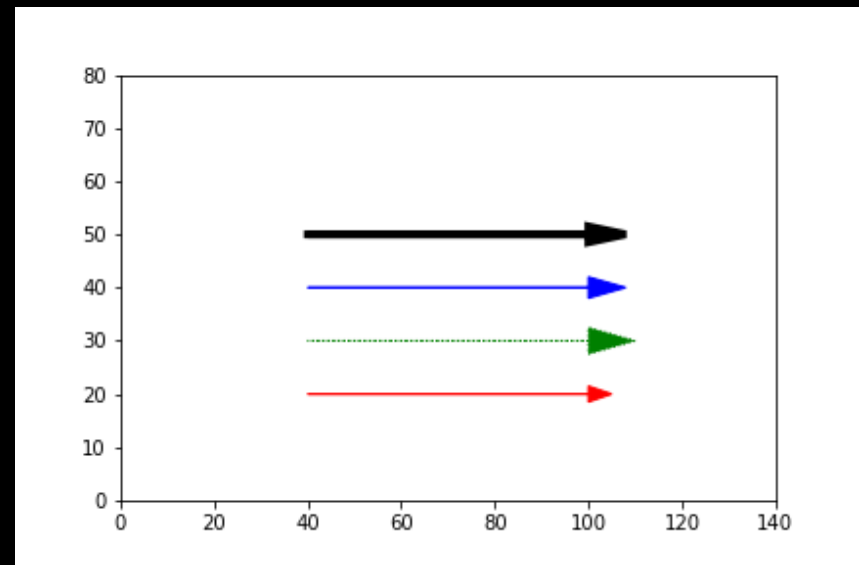
```
plt.arrow(x, y, Δx, Δy, linewidth='linewidth', head_length = 'headlength',  
          head_width = 'headwidth', color = 'color', linestyle = 'linestyle')
```

```
import numpy as np  
import matplotlib.pyplot as plt
```

```
plt.axis([0,140,0,80])
```

```
plt.arrow(40,20,60,0, linewidth=1, color='r', head_length=5, head_width=3)  
plt.arrow(40,30,60,0, linewidth=1, color='g', linestyle=':', head_length=10, head_width=5)  
plt.arrow(40,40,60,0, linewidth=1, color='b', linestyle='-', head_length=8, head_width=4)  
plt.arrow(40,50,60,0, linewidth=4, color='k', linestyle='-', head_length=8, head_width=3)
```

```
plt.show()
```



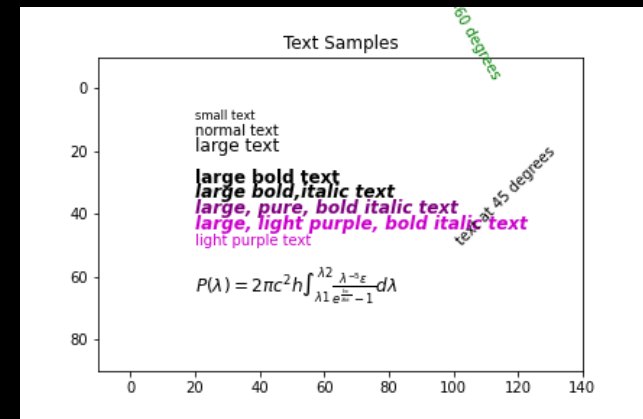


Text

```
plt.text(x,y, 'text', color='color', size='size', fontweight='fontweight',
         fontstyle='fontstyle', rotation=degrees)
```

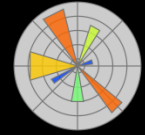
```
import numpy as np
import matplotlib.pyplot as plt

plt.axis([-10,140,90,-10])
plt.axis('on')
plt.grid(False)
plt.title('Text Samples')
plt.text(20,10,'small text',size='small')
plt.text(20,15,'normal text')
plt.text(20,20,'large text',size='large')
plt.text(20,30,'large bold text',size='large',fontweight='bold')
plt.text(20,35,'large bold,italic text',size='large',\
         fontweight='bold', fontstyle='italic')
plt.text(20,40,'large, pure, bold italic text',size='large',\
         fontweight='bold',fontstyle='italic',color=(.5,0,.5))
plt.text(20,45,'large, light purple, bold italic text',size='large',\
         fontweight='bold',fontstyle='italic',color=(.8,0,.8))
plt.text(20,50,'light purple text',color=(.8,0,.8))
plt.text(100,50,'text at 45 degrees',rotation=45,color='k')
plt.text(90,-3,'text at -60 degrees',rotation=-60,color='g')
plt.text(20,65,r'$P(\lambda)=2 \pi c^2 h \int_{\lambda_1}^{\lambda_2} \frac{\lambda^{-5}}{e^{\frac{hc}{\lambda k T}}-1} d\lambda$',size='large')
plt.show()
```





NumPy



Advanced Matplotlib Concepts

rcParams

It contains all Matplotlib settings that are used to create the default styles of the figures. You import it directly from the matplotlib namespace:

```
>>>from matplotlib import rcParams
>>> rcParams
...
'axes.grid': False,
'axes.grid.axis': 'both',
'axes.grid.which': 'major',
'axes.labelcolor': 'black',
'axes.labelpad': 4.0,
'axes.labelsize': 'medium',
'axes.labelweight': 'normal',
'axes.linewidth': 0.8,
...

rcParams['figure.figsize'] = 8, 6
rcParams['legend.fontsize'] = "large"
rcParams['xtick.major.size'] = 4
rcParams['xtick.minor.size'] = 1
```



NumPy

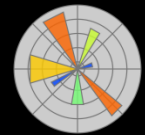


Advanced Matplotlib Concepts

`Get_* functions`

The key to a great plot is customization. To achieve this, you should know how to extract the components you want to customize.

```
>>> import matplotlib.pyplot as plt
>>> fig, ax = plt.subplots()
>>> [func for func in dir(ax) if func.startswith("get")]
['get_adjustable',
 'get_agg_filter',
 'get_alpha',
 'get_anchor',
 'get_animated',
 'get_aspect',
 'get_autoscale_on',
 'get_autoscalex_on',
```



Advanced Matplotlib Concepts

Get_* functions

If you want to customize the xticks of this plot

```
import matplotlib.pyplot as plt  
import numpy as np
```

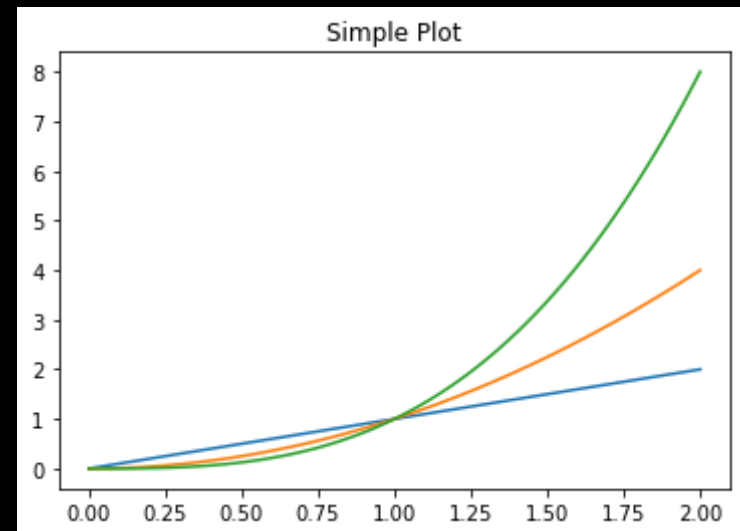
```
x = np.linspace(0, 2, 100)
```

```
fig, ax = plt.subplots() # Create a figure and an axes.
```

```
ax.plot(x, x, label="linear")  
ax.plot(x, x ** 2, label="quadratic")  
ax.plot(x, x ** 3, label="cubic")
```

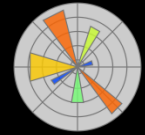
```
ax.set_title("Simple Plot")
```

```
plt.show()
```





NumPy



Advanced Matplotlib Concepts

Get_* functions

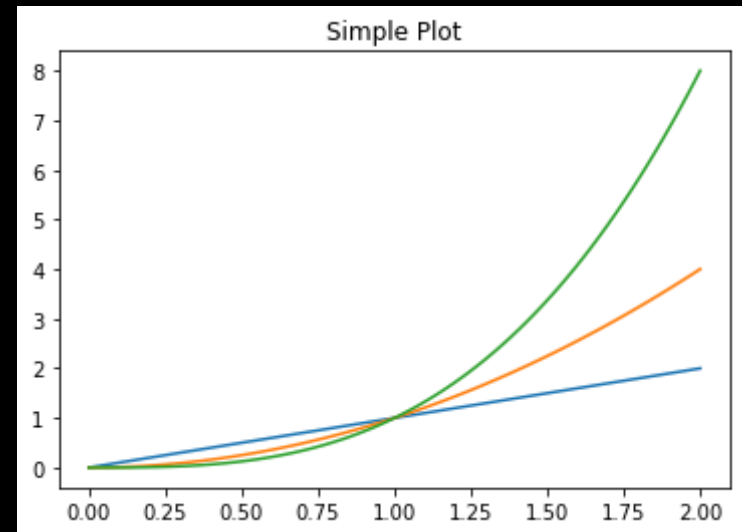
If you want to customize the xticks of this plot

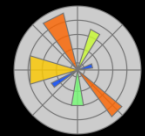
```
>>> ax.get_xticklabels()
```

```
[Text(-0.25, 0, '-0.25'),  
Text(0.0, 0, '0.00'),  
Text(0.25, 0, '0.25'),  
Text(0.5, 0, '0.50'),  
Text(0.75, 0, '0.75'),  
Text(1.0, 0, '1.00'),  
Text(1.25, 0, '1.25'),  
Text(1.5, 0, '1.50'),  
Text(1.75, 0, '1.75'),  
Text(2.0, 0, '2.00'),  
Text(2.25, 0, '2.25')]
```

```
>>> ax.get_xticks()
```

```
array([-0.25,  0.   ,  0.25,  0.5  ,  0.75,  1.   ,  1.25,  1.5  ,  1.75,  
        2.   ,  2.25])
```





Advanced Matplotlib Concepts

getp / setp

```
import matplotlib.pyplot as plt  
import numpy as np
```

```
x = np.linspace(0, 2, 100)
```

```
fig, ax = plt.subplots() # Create a figure and an axes.
```

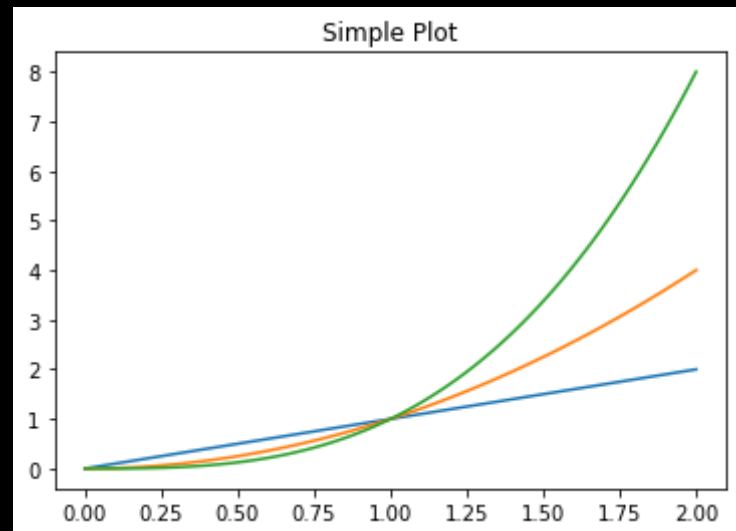
```
l1 = ax.plot(x, x, label="linear")
```

```
l2 = ax.plot(x, x ** 2, label="quadratic")
```

```
l3 = ax.plot(x, x ** 3, label="cubic")
```

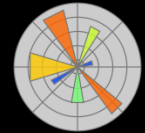
```
ax.set_title("Simple Plot")
```

```
plt.show()
```





NumPy



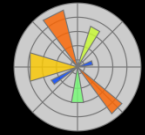
getp / setp

Advanced Matplotlib Concepts

```
plt.getp(12)
agg_filter = None
alpha = None
animated = False
antialiased or aa = True
.
.
.
rasterized = False
sketch_params = None
snap = None
solid_capstyle = projecting
solid_joinstyle = round
transform = CompositeGenericTransform( TransformWrapper( ...
transformed_clip_path_and_affine = (None, None)
url = None
visible = True
xdata = [0.          0.02020202 0.04040404 0.06060606 0.080...
xydata = [[0.          0.          ] [0.02020202 0.00040812] ...
ydata = [0.          0.00040812 0.00163249 0.00367309 0.006...
zorder = 2
```





NumPy



Advanced Matplotlib Concepts

getp / setp



```
plt.setp(12)
    agg_filter: a filter function, which takes a (m, n, 3) float array and a dpi
value, and returns a (m, n, 3) array
    alpha: scalar or None
    animated: bool
    antialiased or aa: bool
    clip_box: `.Bbox`
    clip_on: bool
    clip_path: Patch or (Path, Transform) or None
    color or c: color
    label: object
    linestyle or ls: {'-', '--', '-.', ':', '', (offset, on-off-seq), ...}
    linewidth or lw: float
    marker: marker style string, `~.path.Path` or `~.markers.MarkerStyle`
    markeredgecolor or mec: color
    markeredgewidth or mew: float
    markerfacecolor or mfc: color
    markerfacecoloralt or mfcalt: color
    markersize or ms: float
    markevery: None or int or (int, int) or slice or list[int] or float or (float,
float) or list[bool]
    path_effects: `.AbstractPathEffect`
    picker: float or callable[[Artist, Event], tuple[bool, dict]]
```



NumPy



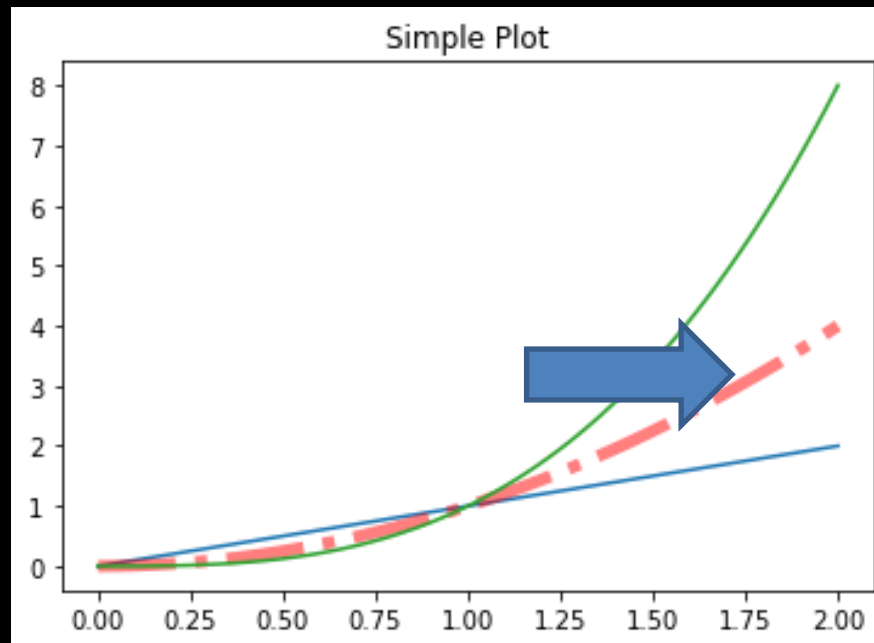
Advanced Matplotlib Concepts

getp / setp

```
>>> plt.setp(l2, "linestyle")
linestyle: {'-', '--', '-.', ':', '', (offset, on-off-seq), ...}

>>> plt.setp(l2, linestyle="-.", lw=5, color="red", alpha=0.5)
[None, None, None, None]

>>> fig.get_figure()
```





NumPy



Legends

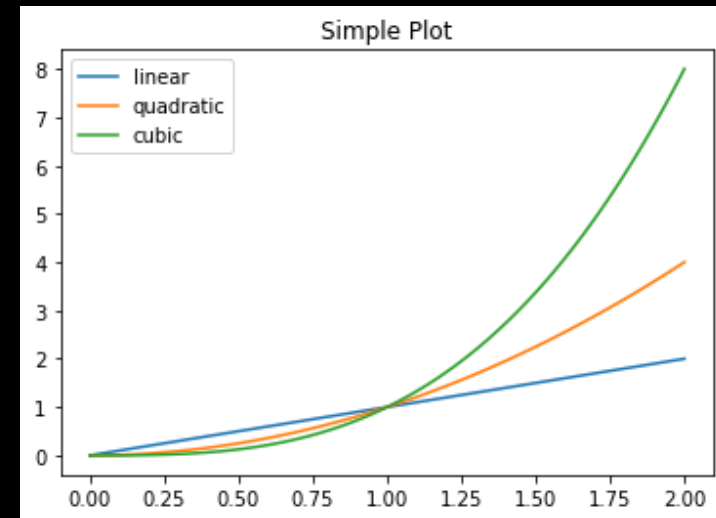
```
import matplotlib.pyplot as plt  
import numpy as np
```

```
x = np.linspace(0, 2, 100)
```

```
fig, ax = plt.subplots() # Create a figure and an axes.
```

```
l1 = ax.plot(x, x, label="linear")  
l2 = ax.plot(x, x ** 2, label="quadratic")  
l3 = ax.plot(x, x ** 3, label="cubic")
```

```
ax.set_title("Simple Plot")  
ax.legend()  
plt.show()
```





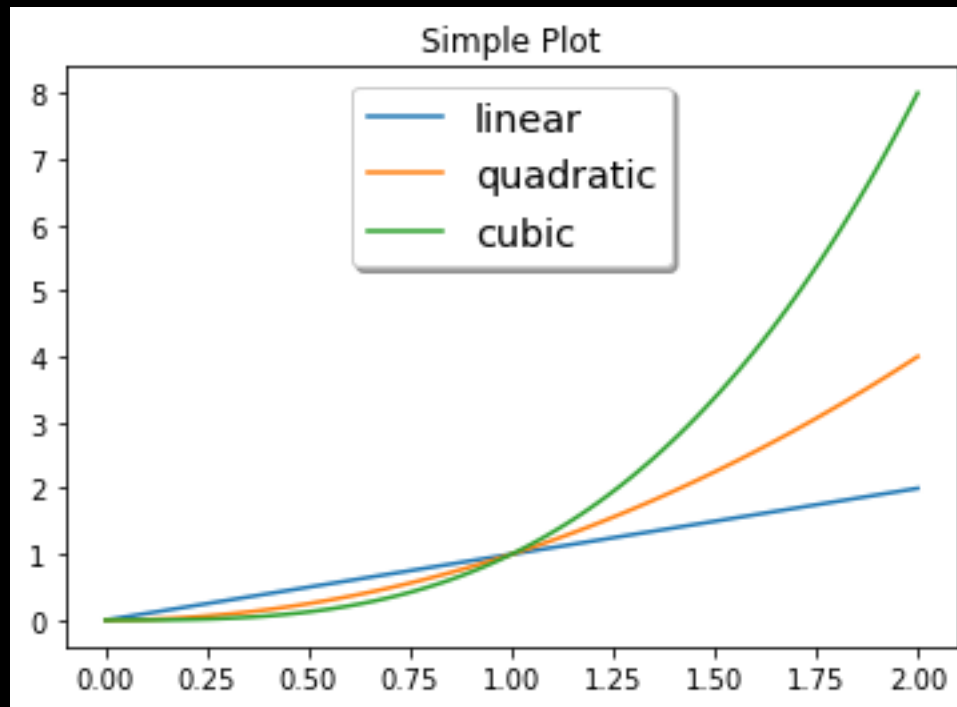
NumPy

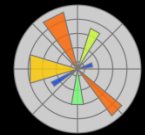
Legends



Advanced Matplotlib Concepts

```
ax.legend(loc='upper center', shadow=True, fontsize='x-large')
```





Advanced Matplotlib Concepts

Cycler

Matplotlib changes its colors or cycles through different styles all by itself.
Matplotlib uses Python built-in objects called Cyclers.

```
from cycler import cycler
```

```
c1 = cycler(arg1=[1, 2, 3, 4])
```

```
c2 = cycler(arg2=list("rgba"))
```

```
for i in c2:  
    print(i)
```

```
for i in c1 + c2:  
    print(i)
```

```
{'arg2': 'r'}
```

```
{'arg2': 'g'}
```

```
{'arg2': 'b'}
```

```
{'arg2': 'a'}
```

```
{'arg1': 1, 'arg2': 'r'}
```

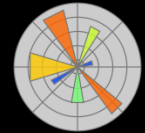
```
{'arg1': 2, 'arg2': 'g'}
```

```
{'arg1': 3, 'arg2': 'b'}
```

```
{'arg1': 4, 'arg2': 'a'}
```



NumPy



Advanced Matplotlib Concepts

Cycler

Matplotlib changes its colors or cycles through different styles all by itself.
Matplotlib uses Python built-in objects called Cyclers.

```
from cycler import cycler

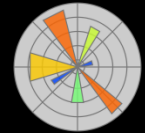
line_prop_cycler = (
    cycler(color=list("rgcy"))
    + cycler(ls=["-", "--", "-.", ":"])
    + cycler(lw=[3, 6, 9, 12])
)

for i in line_prop_cycler:
    print(i)

{'color': 'r', 'ls': '-', 'lw': 3}
{'color': 'g', 'ls': '--', 'lw': 6}
{'color': 'c', 'ls': '-.', 'lw': 9}
{'color': 'y', 'ls': ':', 'lw': 12}
```




NumPy



Cycler

```
import numpy as np
import matplotlib.pyplot as plt
```

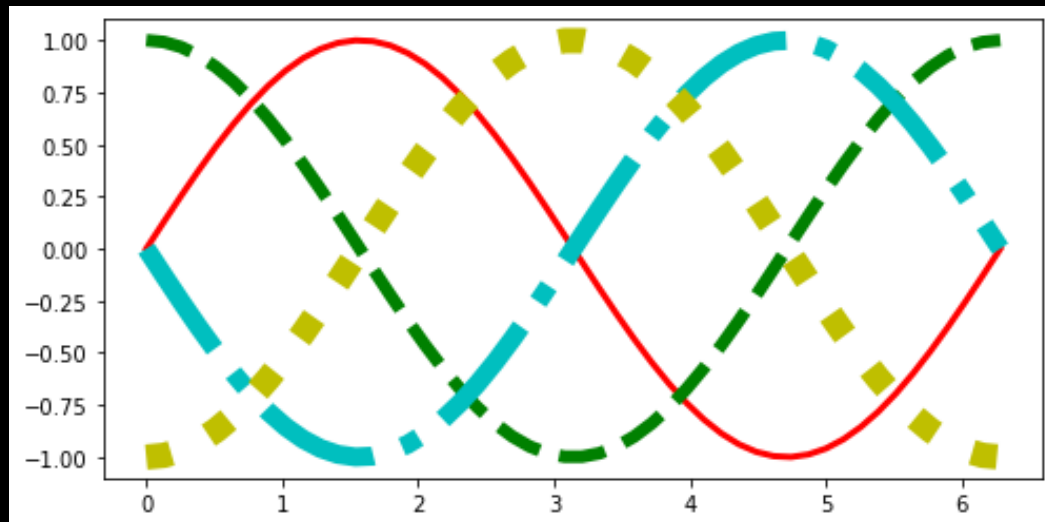
```
x = np.linspace(0, 2 * np.pi, 50)
offsets = np.linspace(0, 2 * np.pi, 4, endpoint=False)
yy = np.transpose([np.sin(x + phi) for phi in offsets])
```

```
fig, ax = plt.subplots(figsize=(8, 4))
```

➔

```
ax.set_prop_cycle(line_prop_cycler) # Set propcycle before plotting
ax.plot(x, yy)
```

```
plt.show();
```





NumPy



Advanced Matplotlib Concepts

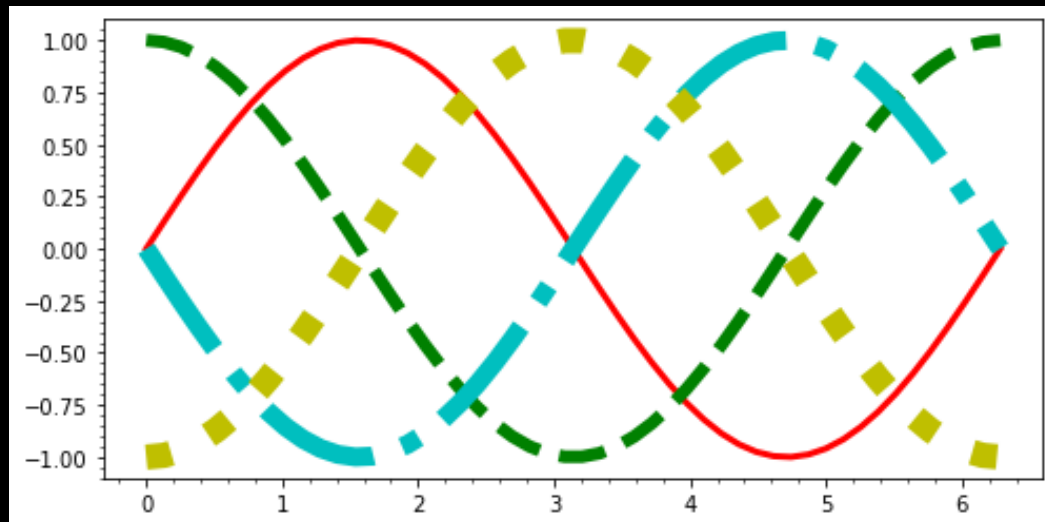
`tick_params`

```
import numpy as np
import matplotlib.pyplot as plt
```

```
x = np.linspace(0, 2 * np.pi, 50)
offsets = np.linspace(0, 2 * np.pi, 4, endpoint=False)
yy = np.transpose([np.sin(x + phi) for phi in offsets])
```

```
fig, ax = plt.subplots(figsize=(8, 4))
```

```
ax.set_prop_cycle(line_prop_cycler) # Set propcycle before plotting
ax.plot(x, yy)
ax.minorticks_on()
plt.show();
```



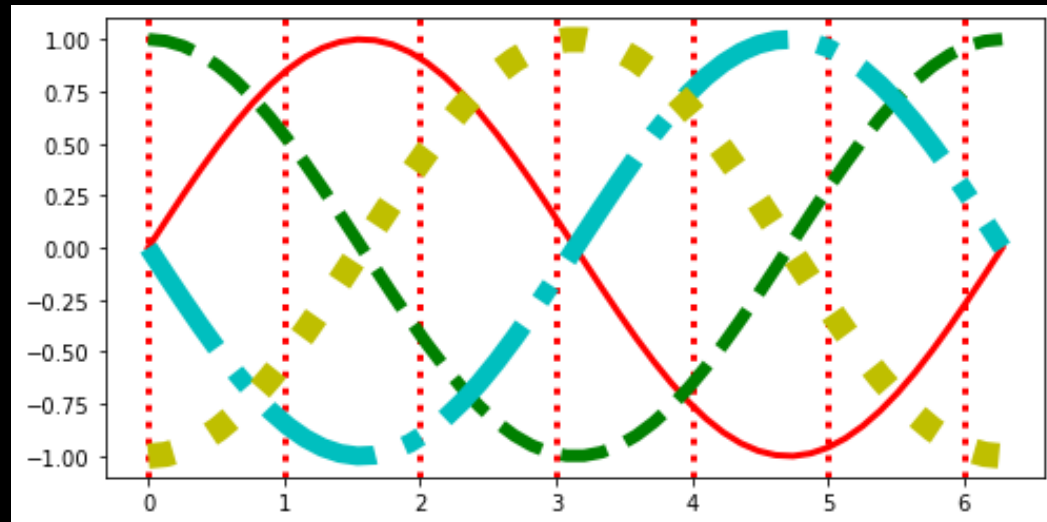


NumPy

Adding custom grids

```
import numpy as np
import matplotlib.pyplot as plt
```

```
x = np.linspace(0, 2 * np.pi, 50)
offsets = np.linspace(0, 2 * np.pi, 4, endpoint=False)
yy = np.transpose([np.sin(x + phi) for phi in offsets])
fig, ax = plt.subplots(figsize=(8, 4))
ax.set_prop_cycle(line_prop_cycler) # Set propcycle before plotting
ax.plot(x, yy)
ax.grid(axis="x", linestyle=":", lw=3, color="r")
plt.show();
```





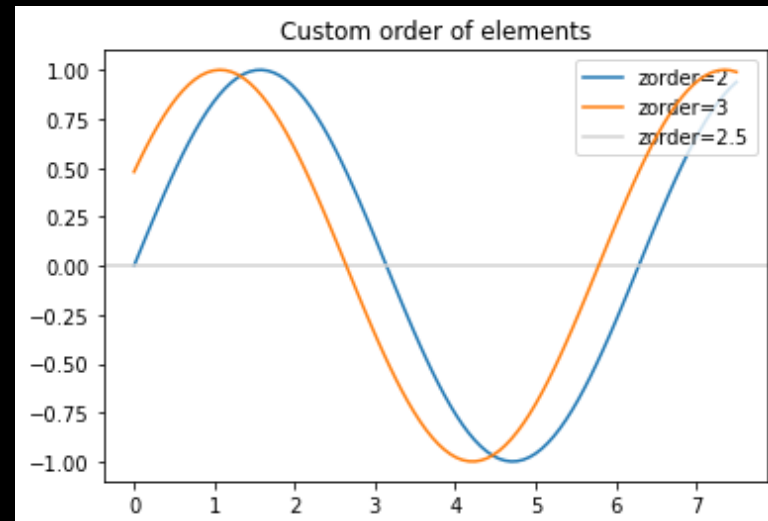
NumPy

Zorder

make sure that each plot gets drawn on the canvas in proper order

```
import numpy as np
import matplotlib.pyplot as plt

x = np.linspace(0, 7.5, 100)
plt.plot(x, np.sin(x), label="zorder=2", zorder=2) # bottom
plt.plot(x, np.sin(x + 0.5), label="zorder=3", zorder=3)
plt.axhline(0, label="zorder=2.5", color="lightgrey", zorder=2.5)
plt.title("Custom order of elements")
l = plt.legend(loc="upper right")
# legend between blue and orange line
l.set_zorder(2.5)
plt.show()
```



Displacement - Velocity

The **displacement** $\Delta x(t_1)$ over the time interval from $t = t_1$ to $t = t_1 + \Delta t$ is defined as:

$$\Delta x(t_1) = x(t_1 + \Delta t) - x(t_1)$$

The displacement is read directly from the motion diagram as the length of the line from $x(1 \text{ s})$ to $x(2 \text{ s})$. The displacement has a direction—it is the displacement from $x(t_i)$ to $x(t_i + \Delta t)$.

The **average velocity** from $t = t_1$ to $t = t_1 + \Delta t$ is:

$$\hat{v}(t_i) = \frac{x(t_1 + \Delta t) - x(t_1)}{\Delta t} = \frac{\Delta x(t_1)}{\Delta t}$$

The average velocity has units meters per second, m/s.

Velocity - Acceleration

The velocity may also vary throughout the motion. As we introduced the velocity to characterize the rate of change of position, we introduce the acceleration to characterize the rate of change of the velocity:

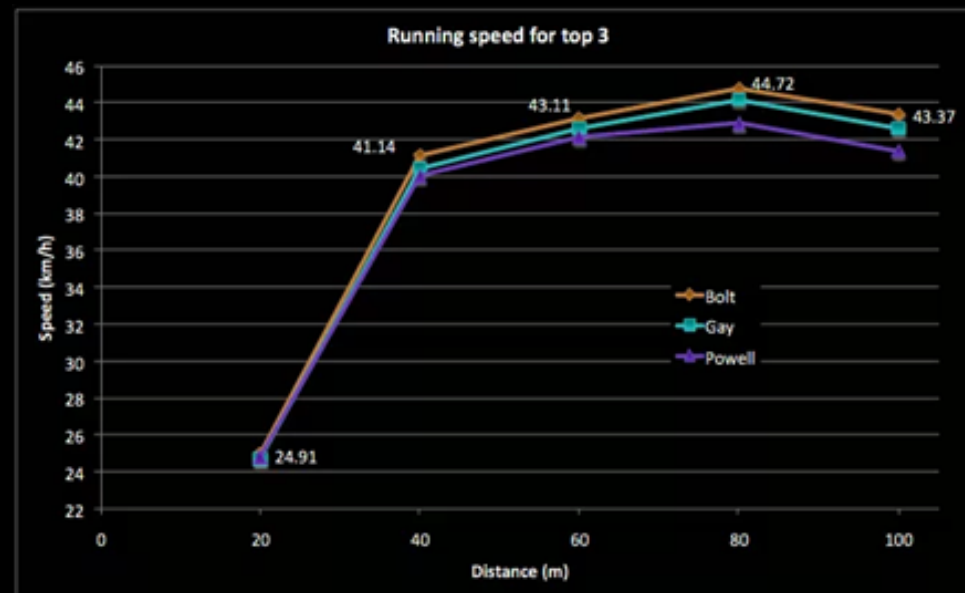
The **average acceleration** over a time interval Δt from t to $t + \Delta t$ is:

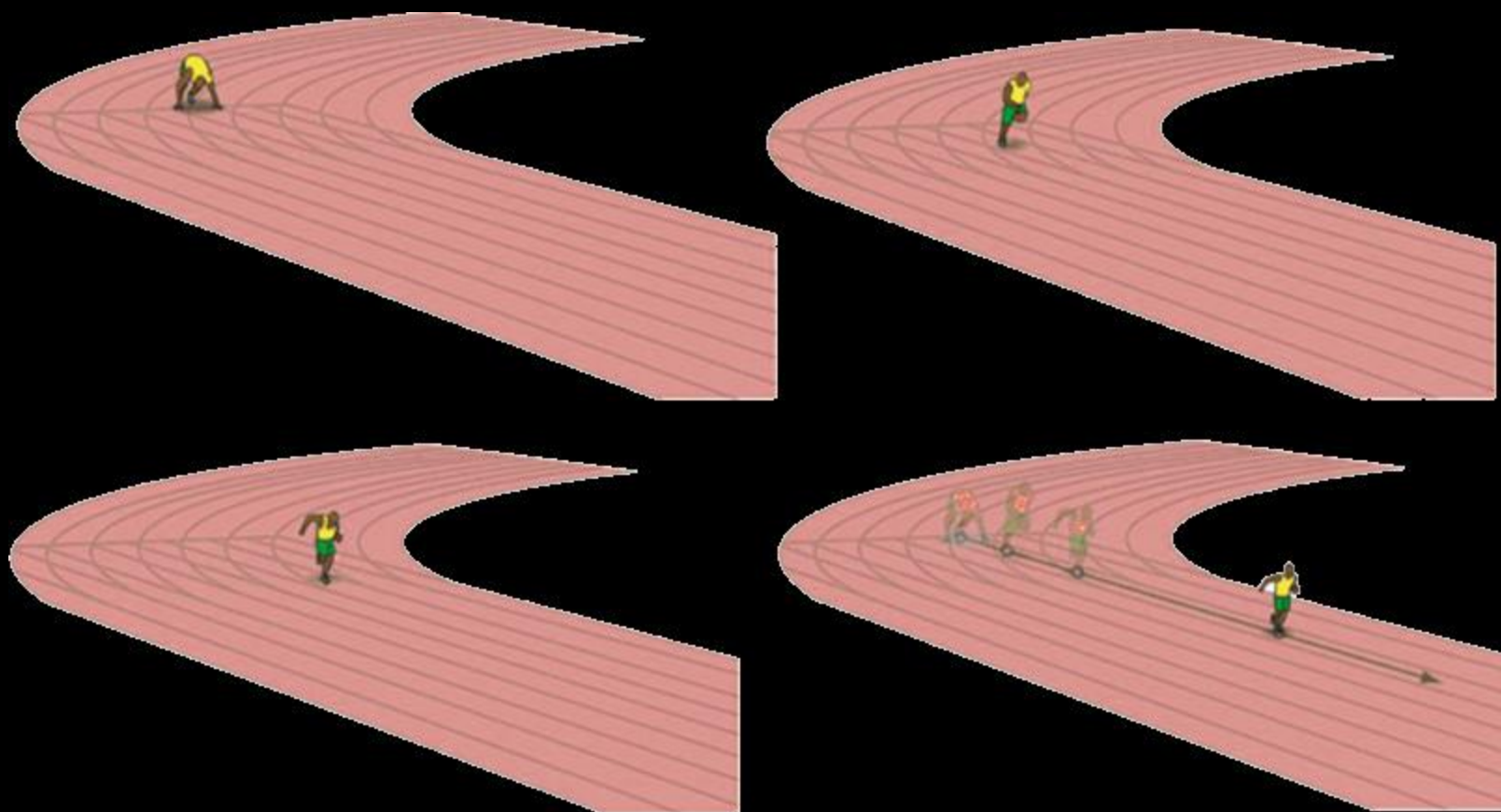
$$\hat{a}(t_i) = \frac{v(t_1 + \Delta t) - v(t_1)}{\Delta t} = \frac{\Delta v(t_1)}{\Delta t}$$

The average acceleration has units meters per second squared, m/s^2 .

0 km/h

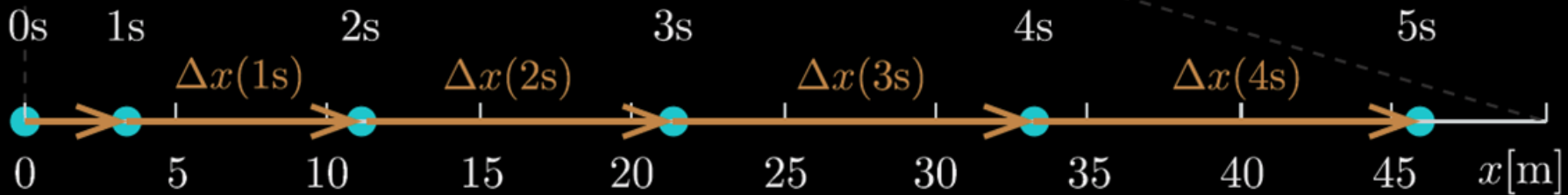
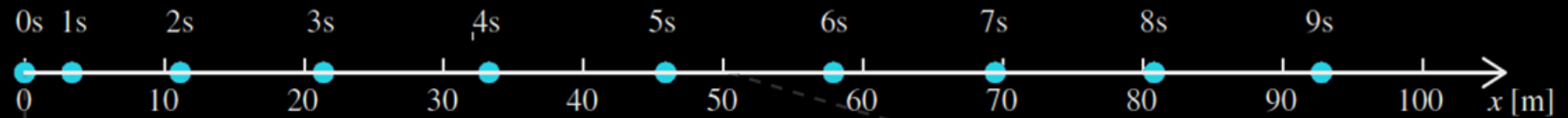
0 mph

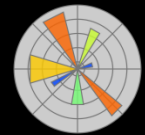






i	0	1	2	3	4	5	6
t_i (s)	0.0	1.0	2.0	3.0	4.0	5.0	6.0
x_i (m)	0.0	3.4	11.1	21.3	33.2	45.8	57.9





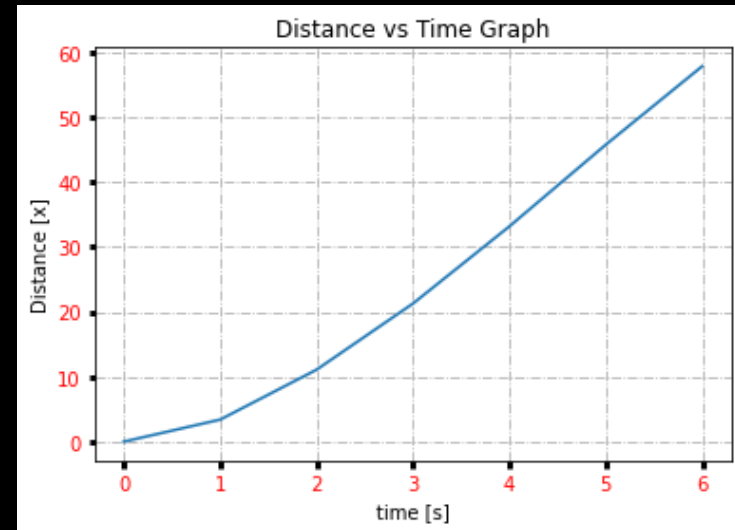
```
import matplotlib.pyplot as plt
import numpy as np
# Data for plotting
t = np.array([0.0, 1.0, 2.0, 3.0, 4.0, 5.0, 6.0])
x = np.array([0.0, 3.4, 11.1, 21.3, 33.2, 45.8, 57.9])
```

```
fig, ax = plt.subplots()
ax.plot(t, x)

ax.set(xlabel='time [s]', \
       ylabel='Distance [x]', \
       title='Distance vs Time Graph')

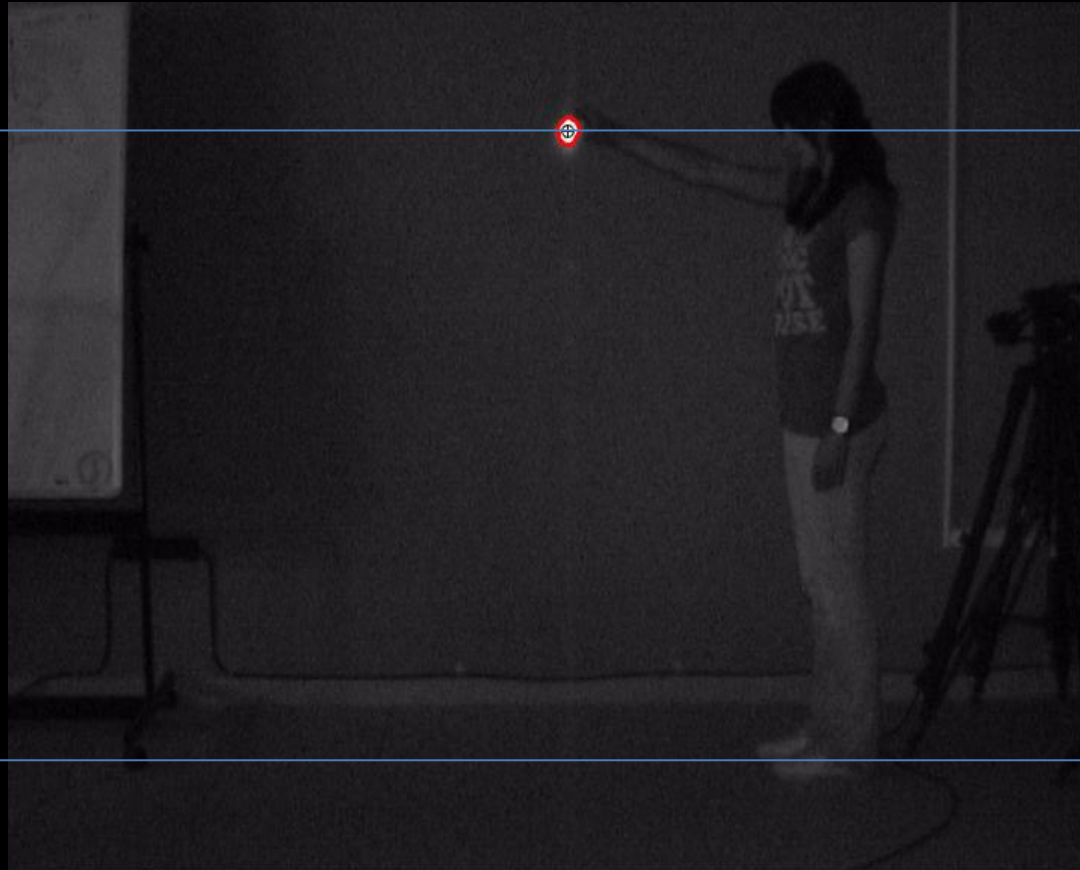
ax.grid(True, linestyle='-.')
ax.tick_params(labelcolor='r', \
               labelsizes='medium', \
               width=3)

plt.show()
```



Free Fall of an Object

How to calculate velocity and accelerations



X	Y
56.77	159.06
56.74	159.10
56.70	158.85
56.64	158.37
56.53	157.37
56.47	156.11
56.38	154.33
56.30	152.21
56.21	149.65
56.12	146.74
56.03	143.33
55.94	139.58
55.87	135.39
55.80	130.86
55.72	125.80
55.63	120.48
55.56	114.61
55.50	108.47
55.41	101.82
55.38	94.85
55.27	87.41
55.17	79.67
55.07	71.47
55.00	63.06
54.92	54.11
54.79	44.90
54.73	35.26
54.69	25.35
54.61	15.05
54.58	4.53



Free Fall of an Object

How to calculate velocity and accelerations

i	t_i (s)	y_i (m)	Δy_i (m)	\bar{v}_i (m/s)	\bar{a}_i (m/s ²)
1	0.0	1.60	-0.05	-0.5	
2	0.1	1.55	-0.15	-1.5	-10.0
3	0.2	1.40	-0.24	-2.4	-9.0
4	0.3	1.16	-0.34	-3.4	-10.0
5	0.4	0.82	-0.43	-4.3	-9.0
6	0.5	0.39			

Free Fall of an Object

How to calculate velocity and accelerations

The average velocities can be calculated from the data: For each i in Table we calculate the average velocity from t_i to t_{i+1} using:

$$v_i = \frac{y_{i+1} - y_i}{\Delta t}$$

The velocities are increasing in magnitude since the ball is accelerating downward. We estimate the average accelerations by

$$a_i = \frac{v_i - v_{i+1}}{\Delta t}$$



Free Fall of an Object

How to calculate velocity and accelerations

```
import matplotlib.pyplot as plt
import numpy as np

x, y = np.loadtxt('dropxy.txt', delimiter=',', usecols=[0,1],unpack=True )
n = len(x)
delta_t = 1/50          # 50 frames per second
time = np.linspace(0, (n-1)*delta_t, n)

vy = np.zeros(n-1, float)
for i in range(n-1):
    vy[i] = (y[i+1] - y[i])/delta_t

ay = np.zeros(n-2, float)
for i in range(n-2):
    ay[i] = (vy[i+1] - vy[i])/delta_t
```



Free Fall of an Object

How to calculate velocity and accelerations

```
fig, (ax1,ax2,ax3)= plt.subplots(3, 1)
```

```
ax1.plot(time, y, 'o-')  
ax1.set_ylabel('y[cm]')
```

```
ax2.plot(time[0:n-1],vy, '.-')  
ax2.set_ylabel('vy [cm/s]')
```

```
ax3.plot(time[1:n-1],ay, '.-')  
ax3.set_ylabel('ay [cm/s^2]')  
ax3.set_xlabel('time (s)')
```

```
plt.show()
```

